## EASTERN UNIVERSITY, SRI LANKA

## FIRST EXAMINATION IN SCIENCE - 2009/2010

FIRST SEMESTER (PROPER/REPEAT)

## (June 2011) PH 101 MECHANICS I

Time: 01 hour.
Answer ALL Questions


1. (a) Distinguish between average velocity and instantaneous velocity. Under what condition is the average velocity equal to instantaneous velocity.

A particle located at position $x=0$ at time $t=0$ starts moving along the positive $x$-direction with a velocity $v$ that varies as $v=k \sqrt{x}$. How do the displacement, velocity and acceleration of the particle vary with time $t$ ? What is the average velocity of the particle if it moves to a distance $d$ in time $t$ from rest?
(b) A particle is moving in two dimensions and its position is given by the polar coordinates $(r, \theta)$. Show that the velocity $v$ and the acceleration $a$ of the particle are given by:

$$
\begin{gathered}
v=\dot{r} e_{r}+r \dot{\theta} e_{\theta} \\
a=\left(\ddot{r}-r \dot{\theta}^{2}\right) e_{r}+(r \ddot{\theta}+2 \dot{r} \dot{\theta}) e_{\theta}
\end{gathered}
$$

where $e_{r}$ and $e_{\theta}$ are the unit vectors along and perpendicular to the radial direction respectively.
2. Explain briefly what you mean by Kinetic energy, Potential energy, Work done, Work-Energy principal and Conservative force.
A particle with unit mass which is initially at rest, moves under the action of a force:

$$
F=\left[\left(3 t^{2}+1\right) \vec{\imath}+(2 t+3) \vec{\jmath}+4 \vec{k}\right] N \text { where } t \text { is in sec. }
$$

i. Express the Newton's second law of motion and write down its mathematical representation.
ii. Find the acceleration of the particle in terms of time $t$.
iii. Find the velocity of the particle at time $t=1$ and $t=2$.
iv. Determine the work done by the force when the particle moves from one point to another, in a time interval $t=1$ and $t=2$.
v. Find the kinetic energy of the particle at time $t=1$ and $t=2$.
vi. Verify the Work-energy theorem using your results for the previous parts.

