EASTERN UNIVERSITY, SRI LANKA

FIRST EXAMINATION IN SCIENCE - 2009/2010

FIRST SEMESTER (PROPER/REPEAT)

(June 2011)

PH 101 MECHANICS I

Time: 01 hour.

Answer ALL Questions



1. (a) Distinguish between average velocity and instantaneous velocity. Under what condition is the average velocity equal to instantaneous velocity.

A particle located at position x=0 at time t=0 starts moving along the positive x-direction with a velocity v that varies as $v=k\sqrt{x}$. How do the displacement, velocity and acceleration of the particle vary with time t? What is the average velocity of the particle if it moves to a distance d in time t from rest?

(b) A particle is moving in two dimensions and its position is given by the polar coordinates (r, θ) . Show that the velocity v and the acceleration a of the particle are given by:

$$v = \dot{r}e_r + r\dot{\theta}e_{\theta}$$

$$a = (\ddot{r} - r\dot{\theta}^2)e_r + (r\ddot{\theta} + 2\dot{r}\dot{\theta})e_{\theta}$$

where e_r and e_θ are the unit vectors along and perpendicular to the radial direction respectively.

2. Explain briefly what you mean by Kinetic energy, Potential energy, Work done, Work-Energy principal and Conservative force.

A particle with unit mass which is initially at rest, moves under the action of a force:

$$F = [(3t^2 + 1)\vec{i} + (2t + 3)\vec{j} + 4\vec{k}]N$$
 where t is in sec.

- i. Express the Newton's second law of motion and write down its mathematical representation.
- ii. Find the acceleration of the particle in terms of time t.
- iii. Find the velocity of the particle at time t = 1 and t = 2.
- iv. Determine the work done by the force when the particle moves from one point to another, in a time interval t=1 and t=2.
 - v. Find the kinetic energy of the particle at time t = 1 and t = 2.
 - vi. Verify the Work-energy theorem using your results for the previous parts.