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EASTERN UNIVERSITY, SRI LANKA DEPARTMENT OF MATHEMATICS THIRD YEAR EXAMINATION IN SCIENCE -2010/2011 FIRST SEMESTER- (April, 2013) MT 305 – OPERATIONAL RESEARCH

Answer all questions.

Time: Three hours.

01. A company manufactures three types of bicycles A, B and C. Each bicycle passes through three departments: Fabrication, Painting & Plating, and Final Assembling. The relevant manufacturing data are given in the table as follows.

Departments	Labor hours per Bicycle			Maximum labor hours	
	A	B	С	available per day	
Fabrication	3	4	5	120	
Painting & Plating	5	3	5	130	
Final Assembling	4	3	5	120	
Profit (in \$) per Bicycle	80	100	70 '		

- (a) Build up a linear programming model for the problem of deciding how many of each type of bicycle to be produced to maximize the profit.
- (b) Use the Simplex method to find the optimal solution for the above linear programming model.
- (c) What is the maximum profit?
- (d) Discuss the effect of the solution in part (b), when the profit on the type C bicycle increases to \$110 with all other data in part (a) remains the same.

02. Consider the following linear programming model.

Minimize

$$Z = 7X_1 + 2X_2$$

subject to the constraints:

$$\begin{split} & 2X_1 + 4X_2 \geq 5, \\ & 8X_1 + 4X_2 \geq 8, \\ & 3X_1 + 8X_2 \geq 4, \\ & 3X_1 - 2X_2 \geq 4, \end{split}$$

where $X_1, X_2 \ge 0$.

- (a) Discuss the possibility and advantages of applying Dual Simplex method for this model.
- (b) Defining variables clearly, construct the dual of this primal.
- (c) Find the solutions of the dual constructed in part (b).
- (d) Interpret your solutions.

03. Using Revised Simplex method, solve the following linear programming model:

Maximize

$$Z = 2X_1 + 3X_2 - X_3 + 4X_4$$

subject to the constraints:

$$X_1 - 2X_2 + X_4 \leq 10,$$

$$X_1 + X_2 + 2X_3 \leq 16,$$

$$(1/2) X_2 - X_3 - X_4 \leq 8,$$

where $X_1, X_2, X_3, X_4 \ge 0$.

04. A company has four machines M₁, M₂, M₃ and M₄ available for assignment to four tasks T₁, T₂, T₃ and T₄. Any machine can be assigned to any task, and each task requires processing by one machine. The time requires by each machine for processing of each task is given in the table below:

[continued Question 04.]

Maller	Time (Hours) requires by tasks						
Machines -	T ₁	T ₂	T ₃	T_4			
M ₁	1 13 4		7	6			
M ₂	1	11	5	4			
M ₃	6	7	2	8			
M ₄ 1		3	4	9			

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- (a) Formulate a mathematical model for this assignment problem. Clearly define the variables and state the constraints.
- (b) Use Hungarian method to find the optimal assignments that minimize the total processing time.
- (c) Write down the minimum total processing time.
- 05. A transporting company plans to transport some logs from three harvesting sites S₁, S₂ and S₃ to three sawmills M₁, M₂ and M₃ at the minimum cost. The distance from each site to each sawmill, number of truckloads of logs available at each site and number of truckloads of logs each sawmill demands, are given in following table. The average cost of transportation is \$2 per kilometer for both loaded and empty trucks.

Logging sites	Distance to mills(in km)			Maximum truckloads	
	\mathbf{M}_1	M_2	M_3	from logging site per day	
S ₁	8	15	50	20	
S ₂	10	17	20	30	
S ₃	30	26	15	45	
Mill demand (Truckload per day)	30	35	30	-	

- (a) Defining variables clearly, build up the mathematical model for the above transportation problem.
- (b) Find the initial feasible solution by using Row minima method.
- (c) Check the optimality of the solutions obtained in part (b) by using modified distribution (MODI) method.
- (d) Find the minimum total cost.

06. Consider the road network as in the following figure, where distances (in km) between adjacent cities are summarized. Find the shortest route from city 1 to city 10, by using Systematic method.

