

## inswer all five questions

Time: 03 hours
21. Lal Ltd. had decided to launch an addition to its product range. The new product may be distributed through any combination of the two company warehouses W1 and W2. The available annual production capacities for the new product are:

100 units at Plant P1
200 units at Plant P2
100 units at Plant P3
The three major concentrations of customer demand are at locations D1, D2 and D3 which are estimated to require each year:

90 units at D1
80 units at D2
90 units at D3
The unit production costs amount to Rs.3, Rs.4, Rs. 1 at P1, P2 and P3 respectively. The unit handling costs at the warehouses amount to Rs. 2 and Rs 3 at W1 and W2 respectively.

The unit trucking costs from plant to warehouse and unit delivery cost from warehouse to customer are as follows:

|  | W1 | W2 |
| :---: | :---: | :---: |
| $\mathbf{P 1}$ | 6 | 6 |
| $\mathbf{P 2}$ | 5 | 5 |
| $\mathbf{P 3}$ | 13 | 4 |


|  | D1 | D2 | D3 |
| :---: | :---: | :---: | :---: |
| W1 | 3 | 5 | 8 |
| W2 | 5 | 3 | 9 |

(All costs are in Rs.)
Required:
(a) Determine an optimum production and distribution schedule.
(Note: You are required to use least cost method to get initial basic feasible solution and MODI method to test optimum solution)
(20 Marks)

Q2.
(a) Drive the basic EOQ formula by using following parameters.
$\mathrm{A}=$ Annual demand
$\mathrm{B}=$ Order quantity
C $=$ Cost of ordering for one order
$\mathrm{H}=$ Carrying cost for one item p.a.
(05 Ma
(b) A company uses a special bracket in the manufacture of its products which it orders outside suppliers. The appropriate data are given below:

Demand $=2000$ per annum
Order cost $=$ Rs. 20 per order
Carrying cost $=20 \%$ of item price
Basic item price $=$ Rs. 10 per bracket
The company is offered the following discounts on the basic price:

For order quantities | $400-799$ | less $2 \%$ |  |
| :--- | :--- | :--- |
|  | $800-1599$ | less $4 \%$ |
|  | 1600 and over | less $5 \%$ |

You are required to establish the most economical quantity to order by calculatin following aspects.
(i) Calculate the EOQ using the basic price.
(05 M
(ii) Compare the savings from the lower price and ordering costs and the extra stockholding at each discount point (i.e. 400,800 and 1600 ) with the costs associated with the basic EO
13. Consider the following activities, associated normal time and cost, together with extra cost of saving a day on selected activities.

| Activity | Preceding <br> Activity | Normal cost of <br> activity (in Rs.) | Normal Time <br> (in Days) | Extra cost of reducing <br> normal time by one day <br> (in Rs.) |
| :---: | :---: | :---: | :---: | :---: |
| A | - | 10,000 | 5 | 3,000 |
| B | - | 12,000 | 7 | 2,000 |
| C | - | 5,000 | 9 | 800 |
| D | A,B | 6,000 | 10 | 600 |
| E | B,C | 9,000 | 8 | 2,000 |
| F | C | 5,000 | 6 | 900 |
| G | D,E | 4,000 | 4 | 700 |
| H | D | 3,000 | 3 | 200 |
| I | F,G,H | 5,000 | 7 | 2,200 |
| J | I | 6,000 | 12 | 500 |

No single activity can be reduced by more than a day. In addition, fixed costs will be incurred at the rate of Rs, 800 for every day.

## You are required to:

(a) Find critical paths, using normal times, the time taken and the total cost of completing the project.
(07 Marks)
(b) The shortest time in which the project can be completed and the associated cost.
(07 Marks)
(c) The lowest cost for which the project can be completed and associated time.
(06 Marks)
(Total 20 Marks)

Q4.
(a) Solve the following Linear Program by using the simplex method and interpret the result Maximize $2 \mathrm{X}_{1}+3 \mathrm{X}_{2}+4 \mathrm{X}_{3}$

## Subject to:

$$
\begin{array}{r}
3 X_{1}+X_{2}+4 X_{3} \leq 600 \\
2 X_{1}+4 X_{2}+2 X_{3} \geq 480 \\
2 X_{1}+3 X_{2}+3 X_{3}=540 \\
X_{1}, X_{2} X_{3} \geq 0
\end{array}
$$

(b) You are given the following linear programming model.

Minimize $Z=3000 a+4000 b+8000 c$

## Subject to:

$$
\begin{aligned}
4 a+2 b & \geq 12 \\
4 b+8 c & \geq 16 \\
a, b, c & \geq 0
\end{aligned}
$$

Covert the above model into a maximization model considering its duality.
(Total 20 N
Q5.
(a) A company is faced with the problem of assigning 4 machines to 6 different jobs (one $m$ to one job only). The profit are estimated as follows:

| Job | Machine |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{D}$ |
| $\mathbf{1}$ | 3 | 6 | 2 | 6 |
| $\mathbf{2}$ | 7 | 1 | 4 | 4 |
| $\mathbf{3}$ | 3 | 8 | 5 | 8 |
| $\mathbf{4}$ | 6 | 4 | 3 | 7 |
| $\mathbf{5}$ | 5 | 2 | 4 | 3 |
| $\mathbf{6}$ | 5 | 7 | 6 | 4 |

Required: Solve the problem to maximize the total profits.
b) Management of the Toys Company needs to decide whether to introduce a certain new novelty toy for the upcoming new year season, after which it would be discontinued. The total cost required to produce and market this toy would be Rs $500,000.00$ plus Rs. 15.00 per toy produced. The company would receive revenue of Rs 35.00 for each toy sold.
(i) Assuming that every unit of this toy that is produced is sold, formulate a mathematical model for the profit in terms of number produce and sold.
(ii) Find out the break-even point that this number must exceed to make it worthwhile to introduce this toy.

