## INDEX NUMBER:

# EASTERN UNIVERSITY, SRI LANKA FACULTY OF COMMERCE AND MANAGEMENT FIRST YEAR SECOND SEMESTER EXAMINATION IN <br> ACHELOR OF BUSINESS ADMINISTRATION/ BACHELOR OF COMMERCE - $2017 / 2018$ (January 2020) (PROPER/ REPEAT) COM 1033 BUSINESS STATISTICS 

ulators permitted.
Time: 03 Hours
Answer All Questions on question sheet in the given spaces.

A marketing manager of an enterprise in a particular city is trying to decide whether to introduce a new product into the market or not. Marketing of the new product will be pursued only if the acceptance rate exceeds $30 \%$. A survey was administered to 253 consumers selected randomly in the city. $32 \%$ of the sampled consumers reported that acceptance of the new product. Identify the following for this study.
a) Population:
b) Parameter of interest:
c) Sample:
d) Statistic:
(04 Marks)

A survey of 1264 women asked who their most trusted shopping advisors was. The results were as follows.

| Shopping advisors | $\%$ | Shopping advisors | $\%$ |
| :--- | :---: | :--- | :---: |
| Advertising $\left(\mathrm{X}_{1}\right)$ | 7 | Online user reviews $\left(\mathrm{X}_{5}\right)$ | 13 |
| Friends/family $\left(\mathrm{X}_{2}\right)$ | 45 | Retail web sites $\left(\mathrm{X}_{6}\right)$ | 4 |
| Manufacturer web sites $\left(\mathrm{X}_{3}\right)$ | 5 | Salespeople $\left(\mathrm{X}_{7}\right)$ | 1 |
| News media $\left(\mathrm{X}_{4}\right)$ | 11 | Other $\left(\mathrm{X}_{8}\right)$ | 14 |

a) Describe a variable of interest in this study.
b) What is the level of measurement of the variable you mentioned in part (a).
c) Construct a bar chart to show the above data.
d) What conclusions can you reach concerning women's'most trusted shopping adviso
III) The number of items rejected daily by a manufacturer because of defects was recorded for days. The results are as follows.

| No. Items <br> rejected | Frequency <br> $\left(\mathrm{f}_{\mathrm{i}}\right)$ | Mid-point <br> $\left(\mathrm{X}_{\mathrm{i}}\right)$ | $\mathrm{f}_{\mathrm{i}} \times \mathrm{X}_{\mathrm{i}}$ | $\mathrm{f}_{\mathrm{i}} \times \mathrm{X}_{\mathrm{i}}^{2}$ | Cumulaf <br> frequen |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 up to 10 | 5 |  |  |  |  |
| 10 up to 15 | 3 |  |  |  |  |
| 15 up to 20 | 9 |  |  |  |  |
| 20 up to 25 | 6 |  |  |  |  |
| 25 up to 30 | 2 |  |  |  |  |

a) Complete the above table and use it to answer the questions given below.
b) Calculate the mean number of rejected items.

Interpret the number you calculated above.
c) Calculate the median number of rejected items.

Interpret the number you calculated above.
d) Calculate the most number (mode) of rejected items.

Interpret the number you calculated above.
e) Calculate the standard deviation of rejected items.

Interpret the number you calculated above.
f) Describe the shape of the distribution of number of rejected items based on th calculated above.
02. 1) A foot wear shop sells two types of running shoes, the Mercury and the Racer. The probad given customer will buy the Mercury is 0.40 and the probability the customer will buy 0.30 . The probability that the customer will buy both is 0.10 . Find the probability that a buy either Mercury or Racer?

Interpret the probability you calculated.

A sample of 500 respondents was selected in a large metropolitan area to study consumer behavio with the following results.

| Enjoys Shopping <br> for clothing | Gender |  |
| :---: | :---: | :---: |
|  | Male | Femalle |
| Yes | 136 | 224 |
| No | 104 | 36 |

a) Suppose the respondent chosen is a female. What is the probability that she does not enjo shopping for clothing?
b) Suppose the respondent chosen enjoys shopping for clothing. What is the probability that th respondent is a male?
c) Are enjoying shopping for clothing and the gender of the individual independent? Explain.
(04 Marks)
A study by a Center for Financial Services Innovation showed that only $64 \%$ of income eamers aged 15 and above had a bank account. If a random sample of 8 income earners aged 15 and above selected,
a) Write down the name of probability distribution model you can use to model the number of income carners aged 15 and above has a bank account;
write down the mathematical expression of probability distribution model you mentioned above;
b) find the probability that all 8 have a bank account;
c) find the expected number of income earners aged 15 and above have a bank accour find the standard deviation of income earners aged 15 and above have a bank accou
IV) The department of transportation maintains statistics for mishandled bags per 1000 airline Past records shows airlines had mishandled 7 bags per 1000 passengers.
a) Write down the most appropriate probability distribution model you would be used the probabilities given below.
b) Find the probability that in the next 1000 passengers, airlines have no mishandledt
c) Find the probability that in the next 2000 passengers, airlines have at least 2 misha
03. I) The amount of time a bank teller spends with each customer is normally distributed with minutes and standard deviation of 0.40 minutes.
a) If a customer is selected randomly, what is the probability that the time spent wit at most 3.15 minutes?
b) If a random sample of 16 customers is selected,
write down the sampling distribution of the mean time spent per customer;
find the probability that the mean time spent per customer is in between 2.90 and 3.20 minutes
(05 Marks)
II) A survey study of 1124 mothers who were currently employed full time revealed that 281 mothers were dissatisfied with their work-life balance and 495 mothers:would take a pay cut to spend more time with their kids.
a) Find the point estimate for the population proportion of mothers employed full-time who are dissatisfied with their work-life balance.
b) Find the $95 \%$ confidence interval estimate for the population proportion of mothers employed full-time who are dissatisfied with their work-life balance.

Interpret the above confidence interval:
c) How many mothers employed full time need to be surveyed to have $95 \%$ co estimating population proportion of mothers employed full time who would take spend more time with their kids to within $\pm 0.01$ ?
(Hint: As there is no such study undertaken previously, assume that the population of mothers employed full time who would take a pay cut to spend more time with 0.5)
III) The mean monthly sales of insurance agents in a particular insurance company in rupees d 72. In an attempt to improve sales, a new training programme has been devised. Ten agert randomly selected to participate in the programme. After the completion of training pros sales of the agents in the next month have been recorded in rupees thousands as follows.

```
63, 87, 95, 75, 83,78, 69, 79, 103, 98
```

Do the data provide sufficient evidence at the $5 \%$ level of significance to indicate that programme is successful?

- Use the above information to answer the questions from (a) to (i)
a) Find the sample mean of monthly sales.

Find the sample standard deviation of monthly sales.
b) What is the most appropriate parameter you would consider to test the claim that trainin programme is successful?
c) State the appropriate null and alternative hypotheses to test the claim, the training programme i successful:
$\mathrm{H}_{0}$ :
$H_{1}$ :
d) Write down the appropriate test statistic for the above hypothesis test.
e) Show the rejection region of the above hypothesis test graphically and write down the decision rule for the hypothesis testing.
f) Compute the value for the test statistic you mentioned in part (d).
g) Write down the statistical decision of the hypothesis test and explain.
h) Write down the conclusion of the test.
i) State what was the assumption you made to perform above hypothesis testing.
04. The marketing division of a large supermarket chain would like to use shelf space to predictt food. A random sample of 12 equal sized stores is selected. The following table lists the shel and weekly sales in Rs. 100s.

| Store <br> No. | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shelf <br> Space | 5 | 5 | 5 | 10 | 10 | 10 | 15 | 15 | 15 | 20 |
| Weekly <br> Sales | 16 | 22 | 14 | 19 | 24 | 26 | 23 | 27 | 28 | 26 |

Use this information to answer the questions from (a) to (h).
a) Identify the independent and dependent variables.

Independent Variable (X):

Dependent Variable (Y):

Construct a scatter plot.

Comment on the relationship between X and Y based on the scatter plot constructed above

Complete the following table and use it to answer the following questions:

| Store <br> No. | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{X Y}$ | $\mathbf{X}^{2}$ | $\mathbf{Y}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 01 |  |  |  |  |  |
| 02 |  |  |  |  |  |
| 03 |  |  |  |  |  |
| 04 |  |  |  |  |  |
| 05 |  |  |  |  |  |
| 06 |  |  |  |  |  |
| 07 |  |  |  |  |  |
| 08 |  |  |  |  |  |
| 09 |  |  |  |  |  |
| 10 |  |  |  |  |  |
| 11 |  |  |  |  |  |
| 12 |  |  |  |  |  |

d) Calculate the correlation coefficient.

Interpret the correlation coefficient you calculated.
e) Develop a least squares linear regression model in an attempt to predict the weekly sal by the shelf space:

Compute the regression coefficient, $b_{1}$ (Slope):

Compute the slope $\mathrm{b}_{0}$ (Intercept):

Write down the linear regression model:

Interpret the meaning of $b_{0}$ in the given problem:

Interpret the meaning of $b_{1}$ in the given problem:

Compute the coefficient of determination.

Interpret the coefficient of determination calculated above:

Predict the weekly sales for a shelf space of 16 feet.
(Total 20 Marks)
Rio Cool Spot wants to forecast quarterly demand for a particular brand ice cream for the 2020. The following table gives quarterly demand of ice cream in Kg , over the last three years.

| Year | Demand |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Q1 | Q2 | Q3 | Q4 |
| 2017 | 20 | 40 | 60 | 15 |
| 2018 | 30 | 48 | 78 | 22 |
| 2019 | 52 | 65 | 95 | 35 |

a) Complete the table below by calculating the 4 - Quarter moving averages, Centered moic of demand and Ratio to centered moving average.

| Year | Quarter | Demand $\left(\mathbf{Y}_{t}\right)$ | 4-Quarter <br> Moving <br> Average | Centered <br> 4-Quarter <br> Moving <br> Average | Ratio <br> Cente <br> Mov <br> Aven |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2017 | 01 | 20 |  |  |  |
| 2017 | 02 | 40 |  |  |  |
| 2017 | 03 | 60 |  |  |  |
| 2017 | 04 | 15 |  |  |  |
| 2018 | 01 | 30 |  |  |  |
| 2018 | 02 | 48 |  |  | , |
| 2018 | 03 | 78 |  |  |  |
| 2018 | 04 | 22 |  |  |  |
| 2019 | 01 | 52 |  |  |  |
| 2019 | 02 | 65 |  |  |  |
| 2019 | 03 | 95 |  |  |  |
| 2019 | 04 | 35 |  |  |  |

Calculate the quarterly seasonal indexes using ratio to moving average method by completing the following table:
$\left.\begin{array}{|c|c|c|c|c|c|}\hline \text { Quarter } & & & & & \begin{array}{c}\text { Mean of ratio } \\ \text { to moving } \\ \text { averages } \\ \text { (Seasonal } \\ \text { index) }\end{array}\end{array} \begin{array}{c}\text { Adjusted } \\ \text { Seasonal } \\ \text { index }\end{array}\right]$.

Find the normalization ratio to calculate the adjusted seasonal index.

The estimated demand trend equation is given by:

$$
\hat{Y}_{t}=26.53+3.10 t
$$

Assuming $t=1$ for 2017 -Quarter 1, forecast the demand of ice cream in all quarters in 2020 by completing the following table.

| Quarters <br> $(2020)$ | Value of t | Estimated demand trend for 2020 | Forecasted demand for <br> 2020 |
| :---: | :---: | :---: | :---: |
| 01 |  |  |  |
| 02 |  |  |  |
| 03 |  |  |  |
| 04 |  |  |  |

(Total 18 Marks)

