

EASTERN UNIVERSITY, SRI LANKA
FACULTY OF COMMERCE AND MANAGEMENT

Third Year First Semester Examination in Bachelor of Commerce/ Bachelor of
 Commerce (Specialization in Accounting and Finance)-2016/2017(November 2018)

(Proper/ Repeat/ Re-Repeat)
 DAF 3043 Corporate Finance

Answer All Questions.

Time: Three (03) hours.

Calculator Permitted.

Table Attached.

financial statements of ABC plc Trading Company are given below:

The Income statement for the year ended 31.12.2017

| | Rs. '000 | Rs. '000 |
|-----------------------------|----------|----------|
| Sales | | 2,000 |
| Less : Cost of Sales: | | |
| Opening Stock | 200 | |
| Purchase | 1,200 | |
| | 1,400 | |
| Less: Closing Stock | 300 | 1,100 |
| Gross Profit | | 900 |
| Add: Investment Income | | 50 |
| | | 950 |
| Less: Operating expenses: | | |
| Administration | 300 | |
| Selling & Distribution | 200 | |
| Finance | 30 | 530 |
| Operating Profit Before Tax | | 420 |
| Less: Taxation | | 120 |
| Operating Profit After Tax | | 300 |

The Statement of Financial Position as at 31.12.2017

| Assets | Rs. '000 | Rs. '000 |
|--|-----------------|-----------------|
| Non- Current Assets: | | |
| Property | 950 | |
| Plant and Machinery | 400 | |
| Motor Vehicles | 150 | |
| Furniture and Equipment | 150 | 1,650 |
| Current Assets: | | |
| Stocks | 300 | |
| Debtors | 440 | |
| Cash & Cash Equivalents | 210 | 950 |
| Total | | 2,600 |
| Liabilities | | |
| Capital and Reserves | | |
| Stated Ordinary Share Capital (88,000 shares) | 880 | |
| Stated 10% Preference Share Capital (3,000 shares) | 300 | |
| General Reserve | 260 | |
| Accumulated Profits | 400 | 1,840 |
| Non-Current Liabilities | | |
| 15% Debentures | | 160 |
| Current Liabilities | | |
| Creditors | 280 | |
| Tax Payable | 120 | |
| Dividends Payable | 150 | |
| Administrative expenses payable | 50 | 600 |
| Total | | 2,600 |

The Statement of Changes in Equity for the year ended 31.12.2017

| Items | Ordinary Shares | General Reserve | Accumulated Profit | Total |
|-----------------------------------|-----------------|-----------------|--------------------|----------|
| | Rs. '000 | Rs. '000 | Rs. '000 | Rs. '000 |
| Balance as at 1.1.2017 | 880 | 210 | 300 | 1,300 |
| Profit for 2017 | - | - | 300 | 300 |
| General Reserve | - | 50 | (50) | - |
| Dividends (Ordinary & Preference) | - | - | (150) | (150) |
| Balance as at 31.12.2017 | 880 | 260 | 400 | 1,450 |

The industrial average ratios are as follows:

| | |
|-----------------------------------|-------|
| Gross Profit Margin (%) | 43.50 |
| Net Profit Margin (After Tax) (%) | 14.32 |
| Return on Assets (%) | 10.75 |
| Return on Capital Employed (%) | 15.53 |
| Return on Equity (%) | 16.34 |
| Capital Assets Turnover | 0.82 |
| Net Assets Turnover | 1.74 |
| Non-Current Assets Turnover | 1.25 |
| Current Assets Turnover | 3.35 |
| Stock Turnover (COS/AS) | 4.50 |
| Stock Holding Period (Days) | 80 |
| Debtor Turnover | 5.14 |
| Debtor Collection Period (Days) | 70 |
| Creditor Turnover | 4.23 |
| Creditors Payment Period (Days) | 85 |

| | |
|--------------------------------|-------|
| Current Ratio | 1.60 |
| Quick Ratio | 1.12 |
| Working Capital Ratio | 0.45 |
| Cash Ratio | 0.25 |
| Total Debt to Equity Ratio | 0.70 |
| Long Term Debt to Equity Ratio | 0.31 |
| Fixed Interest Coverage | 19.52 |
| Fixed Dividend Coverage | 11.00 |
| Gearing Ratio | 0.25 |
| Earnings Per Share (Rs.) | 3.00 |
| Dividend Per Share (Rs.) | 1.32 |
| Earnings Yield (%) | 18.28 |
| Dividend yield (%) | 8.75 |
| Price/Earnings ratio | 4.50 |

The Average Market price of an ordinary share of the company was Rs.15 for 2017. All sales and purchases are on credit basis. The business operating days 360.

Required:

Calculate the relevant ratios for ABC plc for the above the financial year and evaluate the company's relative operating performance and financial position comparing industrial average ratios and pointing out the deficiencies and suggest improvements.

- (20 Mar)
02. (I) Suppose a person save in a bank Rs.20,000 a year for 5 years, and Rs.30,000 a year for 7 years thereafter. What will these savings cumulate to at the end of 12 years if the interest rate is 10% compounded annually?
(04 Mar)
- (II) A finance company advertises that it will pay a lump sum of Rs.400,000 at the end of a year to investors who deposit monthly Rs.30,000. What is annual interest rate in this offer if it is compounded monthly?
(04 Mar)
- (III) Suppose a person wants to buy a motor car in five years. He estimates that the vehicle will cost him Rs.5 million when he becomes ready to buy it. How much money would he need to invest each year in an account bearing interest at the rate of 12 percent per year in order to accumulate to amount equivalent to the purchase price of the motor vehicle?
(04 Mar)
- (IV) Suppose an investor estimates the receipt of cash flows of Rs.150,000 at the end of each year for next 5 years and Rs.170,000 and Rs.200,000 respectively at the end of years 6 and 7. Assuming a discount rate of 10% during the next 5 years and 15% thereafter determine the present value of the cash inflows.
(04 Mar)

(V) A firm has borrowed a bank loan of Rs.1 million from a bank. The loan requires five equal end - year payments of Rs.277,410 each towards the repayment of loan with interest. What interest rate does the bank charge? Prepare a loan amortization schedule.

(04 Marks)

(Total 20 Marks)

(I) Giggles Company plans to produce and sell 100,000 baby diapers during the next year at an average price of Rs.25 per unit. Variable manufacturing costs are estimated at Rs.10 per unit, and variable marketing costs at Rs.5 per unit to be sold. Fixed costs are estimated at Rs.500,000 for manufacturing and Rs.200,000 for marketing. There will be no year-end work-in-process inventory. Income taxes are ignored.

Required:

- (a) Calculate the company's Break-Even Points in units and rupees for the year.
- (b) How many units of baby diapers the company should sell in order to earn a net profit of Rs.200,000 during the year?
- (c) Suppose the Company estimates that variable manufacturing costs increases by 10 percent in the coming year. What will be impact on its Break-Even Point?
- (d) If the company's variable manufacturing costs do increase by 10 percent, what should the company do to maintain the same contribution margin ratio in the coming year?

(10 Marks)

GRP plc manufactures a line of electric fans that are sold in general hardware stores. The company's marketing manager, Mr. Bandara, has just received the sales forecast for the coming year 2019 for the GRP's three types of fans: Ceiling Fans, Pedestal Fans, and Cooling Fans. GRP has experienced considerable variations in sales volumes and variable costs over the past two years, and Bandara believes the forecast should be carefully evaluated from a cost-volume-profit viewpoint. The preliminary budget information for the year 2019 is as follows:

| | Ceiling Fans | Pedestal Fans | Cooling Fans |
|---|--------------|---------------|--------------|
| Unit Sales | 1,000 | 700 | 300 |
| Unit Selling Price (Rs) | 3,000 | 4,000 | 3,500 |
| Variable Manufacturing Cost per unit (Rs) | 1,500 | 1,400 | 1,550 |
| Variable Selling Cost per unit (Rs) | 300 | 400 | 200 |

For the year 2019, GRP's fixed manufacturing overhead is budgeted Rs.1,000,000, and the company's fixed selling and administrative expenses are forecasted to be Rs.297,500. GRP has a tax rate of 20 percent.

Required:

- Determine GRP Company's budgeted net income for the year 2019.
- Assuming the sale mix remains as budgeted, determine how many units (nearest real whole figure) of each type of fans GRP must sell in order to break even in the year 2019.
- After preparing the original estimates, management found that its total fixed cost would decrease to Rs.1025,000, and the variable manufacturing cost and selling cost of Cooling Fans decreases by Rs.300 and Rs.50 per unit respectively due to a modification of its manufacturing and selling strategy. In addition, management has learned that its Cooling Fans have been perceived as the best value on the market, and it can expect to sell two times as many Cooling Fans as each of other types of fans keeping the total units of 2,000 unchanged. Under the circumstances, determine how many units (in nearest real whole figure) of each type of fans GRP would have to sell in order to break even in the year 2019.

(10 Marks)
(Total 20 Marks)

- (I) The board of directors of CBK Constructors is considering the purchase of a site for a construction of a children park. The purchase price for the site is Rs.250,000. The construction of park will cost Rs.1250,000. The children park would be usable for 10 years. The board hired a consultant, who estimated the net cash inflow to be Rs.250,000 each for first five years and Rs.300,000 each for the next five years. The Company's cost of capital is 10 percent for this project.

Required:

- (a) Calculate the Net Present Value (NPV) of the project. Should the board approve the project based on the NPV?
- (b) Calculate the Internal Rate of Return (IRR) of the project. Should the board approve the project based on the IRR?

(10 Marks)

The owner of Sun Shines restaurant is considering an expansion of the business.

He has identified two alternatives as follows:

- Build a new restaurant in the town
- Buy and renovate an old building downtown for the new restaurant.

The projected cash flows from these two alternatives are shown below. The projects estimated life is 10 years for the first project and 5 years for the latter.

Depreciation of project is on straight line basis. The owner of the restaurant uses a 12 percent required rate of return. He will consider capital project only if they have a payback period of five years or less. The owner also favors projects that exhibit an accounting rate of return of at least 15 percent.

| Investment Proposal | Cash Outflow: (Rs.) | Net After-Tax Cash Inflows (Rs.) | |
|---------------------|------------------------|-------------------------------------|------------|
| | Time 0 | Years 1-5 | Years 6-10 |
| Town Restaurant | 500,000 | 80,000 | 120,000 |
| Downtown Restaurant | 250,000 | 100,000 | - |

Required: Calculate the following for each alternative restaurant site:

- (a) Net Present Value
- (b) Profitability Index
- (c) Discounted Payback Period
- (d) Accounting Rate of Return based on the average investment and average profits in the projects.
- (e) How do the two projects rank in terms of the above answers?
- (f) If the owner of the restaurant sticks to his criteria, which site will he choose?

(10 Marks)

(Total 20 Marks)

05. (I) The shares of PVC plc have an expected return of 22% and standard deviation of 40%. The shares of QIG plc have expected return of 24% and standard deviation of 38%. PVC plc has a beta of 0.86 and QIG plc 1.24. The correlation between returns from the shares of PVC and QIG is 0.72. The standard deviation of the market return is 20%.

Required:

- (a) Is investing in shares of QIG plc better than investing in shares of PVC plc?
- (b) If an investor invests 30% in shares of QIG plc and 70% in shares of PVC plc, what will be the expected rate of return and the portfolio standard deviation?
- (c) What is the market portfolio's expected rate of return and how much is the risk-free rate?
- (d) What is the beta of portfolio if PVC plc's weight is 70% and QIG plc is 30%?

(10 Marks)

(II) An investor holds an investment on the bonds of SPC plc having a par value of Rs.1000 each with coupon rate of 12% per annum payable annually and the maturity of 10 years.

Required:

- (a) What is the value of a bond today if the market rate of return is equal to the coupon rate?
- (b) What will be the value of the bond if the market interest rate increases to 15% at the end of two years?
- (c) What will be the value of the bond if the market interest rate decreases to 10% at the end of five years?
- (d) If the value of the bond is Rs.1250 after six years from the date of issue, what would be the YTM of the bond?

(10 Marks)

(Total 20 Marks)

Present Value and Future Value Tables

Table A-1 Future Value Interest Factors for One Dollar Compounded at k Percent for n Periods: $FVIF_{k,n} = (1+k)^n$

| Period | 1% | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 20% |
|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | 1.0100 | 1.0200 | 1.0300 | 1.0400 | 1.0500 | 1.0600 | 1.0700 | 1.0800 | 1.0900 | 1.1000 | 1.1100 | 1.1200 | 1.1300 | 1.1400 | 1.1500 | 1.1600 | 1.2000 |
| 2 | 1.0201 | 1.0404 | 1.0609 | 1.0816 | 1.1025 | 1.1236 | 1.1449 | 1.1664 | 1.1881 | 1.2100 | 1.2321 | 1.2544 | 1.2769 | 1.2996 | 1.3225 | 1.3456 | 1.4400 |
| 3 | 1.0303 | 1.0612 | 1.0927 | 1.1249 | 1.1576 | 1.1910 | 1.2250 | 1.2597 | 1.2950 | 1.3310 | 1.3676 | 1.4049 | 1.4429 | 1.4815 | 1.5209 | 1.5609 | 1.7200 |
| 4 | 1.0406 | 1.0824 | 1.1255 | 1.1699 | 1.2155 | 1.2625 | 1.3108 | 1.3605 | 1.4116 | 1.4641 | 1.5181 | 1.5735 | 1.6305 | 1.6890 | 1.7490 | 1.8106 | 2.0700 |
| 5 | 1.0510 | 1.1041 | 1.1593 | 1.2167 | 1.2763 | 1.3382 | 1.4026 | 1.4693 | 1.5386 | 1.6105 | 1.6851 | 1.7623 | 1.8424 | 1.9254 | 2.0114 | 2.1003 | 2.4850 |
| 6 | 1.0615 | 1.1262 | 1.1941 | 1.2653 | 1.3401 | 1.4185 | 1.5007 | 1.5869 | 1.6771 | 1.7716 | 1.8704 | 1.9738 | 2.0820 | 2.1950 | 2.3131 | 2.4364 | 2.9650 |
| 7 | 1.0721 | 1.1487 | 1.2299 | 1.3159 | 1.4071 | 1.5036 | 1.6058 | 1.7138 | 1.8280 | 1.9487 | 2.0762 | 2.2107 | 2.3526 | 2.5023 | 2.6609 | 2.8286 | 3.5850 |
| 8 | 1.0829 | 1.1717 | 1.2668 | 1.3686 | 1.4775 | 1.5938 | 1.7182 | 1.8509 | 1.9926 | 2.1436 | 2.3045 | 2.4760 | 2.6584 | 2.8526 | 3.0590 | 3.2784 | 4.2990 |
| 9 | 1.0937 | 1.1951 | 1.3048 | 1.4233 | 1.5513 | 1.6895 | 1.8385 | 1.9990 | 2.1719 | 2.3579 | 2.5580 | 2.7731 | 3.0040 | 3.2519 | 3.5179 | 3.8030 | 5.0000 |
| 10 | 1.1046 | 1.2190 | 1.3439 | 1.4802 | 1.6289 | 1.7908 | 1.9672 | 2.1599 | 2.3694 | 2.5937 | 2.8394 | 3.1058 | 3.3946 | 3.7072 | 4.0456 | 4.4114 | 6.1910 |
| 11 | 1.1157 | 1.2434 | 1.3842 | 1.5395 | 1.7103 | 1.8983 | 2.1049 | 2.3316 | 2.5804 | 2.8531 | 3.1518 | 3.4785 | 3.8359 | 4.2262 | 4.6524 | 5.1173 | 7.4300 |
| 12 | 1.1268 | 1.2682 | 1.4258 | 1.6010 | 1.7959 | 2.0122 | 2.2522 | 2.5182 | 2.8127 | 3.1384 | 3.4985 | 3.8960 | 4.3345 | 4.8179 | 5.3503 | 5.9360 | 8.9100 |
| 13 | 1.1381 | 1.2936 | 1.4685 | 1.6651 | 1.8856 | 2.1329 | 2.4098 | 2.7196 | 3.0658 | 3.4523 | 3.8833 | 4.3635 | 4.8990 | 5.4924 | 6.1528 | 6.8958 | 10.5900 |
| 14 | 1.1495 | 1.3195 | 1.5126 | 1.7317 | 1.9799 | 2.2609 | 2.5785 | 2.9372 | 3.3417 | 3.7975 | 4.3104 | 4.8871 | 5.5348 | 6.2613 | 7.0757 | 7.9875 | 12.6300 |
| 15 | 1.1610 | 1.3459 | 1.5580 | 1.8009 | 2.0789 | 2.3966 | 2.7590 | 3.1722 | 3.6425 | 4.1772 | 4.7846 | 5.4736 | 6.2543 | 7.1379 | 8.1371 | 9.2655 | 15.4070 |
| 16 | 1.1726 | 1.3728 | 1.6047 | 1.8730 | 2.1829 | 2.5404 | 2.9522 | 3.4259 | 3.9703 | 4.5950 | 5.3109 | 6.1304 | 7.0673 | 8.1372 | 9.3676 | 10.7480 | 18.4800 |
| 17 | 1.1843 | 1.4002 | 1.6528 | 1.9479 | 2.2920 | 2.6928 | 3.1588 | 3.7000 | 4.3276 | 5.0545 | 5.8951 | 6.8660 | 7.9861 | 9.2765 | 10.7610 | 12.4680 | 21.2400 |
| 18 | 1.1961 | 1.4282 | 1.7024 | 2.0258 | 2.4065 | 2.8543 | 3.3799 | 3.9960 | 4.7171 | 5.5599 | 6.5436 | 7.6900 | 9.0243 | 10.5750 | 12.3750 | 14.4630 | 24.2300 |
| 19 | 1.2081 | 1.4568 | 1.7535 | 2.1068 | 2.5270 | 3.0256 | 3.6165 | 4.3157 | 5.1417 | 6.1159 | 7.2633 | 8.6128 | 10.1970 | 12.0560 | 14.2320 | 16.7770 | 27.5000 |
| 20 | 1.2202 | 1.4859 | 1.8061 | 2.1911 | 2.6533 | 3.2071 | 3.8697 | 4.6610 | 5.6044 | 6.7275 | 8.0623 | 9.6463 | 11.5230 | 13.7430 | 16.3670 | 19.6710 | 31.3800 |
| 21 | 1.2324 | 1.5157 | 1.8603 | 2.2785 | 2.7860 | 3.3996 | 4.1406 | 5.0338 | 6.1088 | 7.4002 | 8.9492 | 10.8040 | 13.0210 | 15.6680 | 18.8220 | 22.5740 | 35.5000 |
| 22 | 1.2447 | 1.5460 | 1.9161 | 2.3699 | 2.9253 | 3.6035 | 4.4304 | 5.4365 | 6.6598 | 8.1403 | 9.9336 | 12.1000 | 14.7140 | 17.8610 | 21.6450 | 26.1860 | 40.0000 |
| 23 | 1.2572 | 1.5769 | 1.9736 | 2.4647 | 3.0715 | 3.8197 | 4.7405 | 5.8715 | 7.2579 | 8.9543 | 11.0260 | 13.5520 | 16.6270 | 20.3620 | 24.8910 | 30.3760 | 45.0000 |
| 24 | 1.2697 | 1.6084 | 2.0328 | 2.5633 | 3.2251 | 4.0489 | 5.0724 | 6.3412 | 7.9111 | 9.8497 | 12.2390 | 15.1790 | 18.7880 | 23.2120 | 28.6250 | 35.2380 | 50.5000 |
| 25 | 1.2824 | 1.6406 | 2.0938 | 2.6658 | 3.3864 | 4.2919 | 5.4274 | 6.8495 | 8.6231 | 10.8350 | 13.5850 | 17.0000 | 21.2310 | 26.4620 | 32.9190 | 40.8740 | 56.5000 |
| 30 | 1.3478 | 1.8114 | 2.4273 | 3.2434 | 4.3219 | 5.7435 | 7.6123 | 10.0630 | 13.2680 | 17.4490 | 22.8920 | 29.9600 | 39.1160 | 50.9500 | 66.2120 | 85.8600 | 134.0000 |
| 35 | 1.4166 | 1.9999 | 2.8139 | 3.9461 | 5.5160 | 7.6861 | 10.6770 | 14.7850 | 20.4140 | 28.1020 | 38.5750 | 52.8000 | 72.0690 | 98.1000 | 133.1760 | 180.3140 | 290.0000 |
| 36 | 1.4308 | 2.0399 | 2.8983 | 4.1039 | 5.7918 | 8.1473 | 11.4240 | 15.9680 | 22.2510 | 30.9130 | 42.6180 | 59.1360 | 81.4370 | 111.8340 | 153.1520 | 209.1640 | 340.0000 |
| 40 | 1.4889 | 2.2080 | 3.2620 | 4.8010 | 7.0400 | 10.2860 | 14.9740 | 21.7250 | 31.4090 | 45.2590 | 65.0010 | 93.0510 | 132.7820 | 188.8840 | 267.8640 | 378.7210 | 600.0000 |
| 50 | 1.6446 | 2.6916 | 4.3839 | 7.1067 | 11.4670 | 18.4200 | 29.4570 | 46.9020 | 74.3580 | 117.3910 | 184.5650 | 289.0020 | 450.7360 | 700.2330 | | | |

Table A-2 Future Value Interest Factors for a One-Dollar Annuity Compounded at k Percent for n Periods: $FVIFA_{k,n} = [(1+k)^n - 1] / k$

| Period | 1% | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 20% |
|--------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|----------|----------|----------|------------|----------|----------|----------|
| 1 | 1.0000 | 1.0200 | 1.0300 | 1.0400 | 1.0500 | 1.0600 | 1.0700 | 1.0800 | 1.0900 | 1.1000 | 1.1100 | 1.1200 | 1.1300 | 1.1400 | 1.1500 | 1.1600 | 1.2000 |
| 2 | 2.0100 | 2.0200 | 2.0300 | 2.0400 | 2.0500 | 2.0600 | 2.0700 | 2.0800 | 2.0900 | 2.1000 | 2.1100 | 2.1200 | 2.1300 | 2.1400 | 2.1500 | 2.1600 | 2.2000 |
| 3 | 3.0301 | 3.0604 | 3.0909 | 3.1216 | 3.1525 | 3.1836 | 3.2149 | 3.2464 | 3.2781 | 3.3100 | 3.3421 | 3.3744 | 3.4069 | 3.4396 | 3.4725 | 3.5056 | 3.6400 |
| 4 | 4.0604 | 4.1216 | 4.1836 | 4.2465 | 4.3101 | 4.3744 | 4.4399 | 4.5061 | 4.5731 | 4.6410 | 4.7097 | 4.7793 | 4.8498 | 4.9211 | 4.9934 | 5.0665 | 5.3600 |
| 5 | 5.1010 | 5.2040 | 5.3091 | 5.4163 | 5.5256 | 5.6371 | 5.7507 | 5.8666 | 5.9847 | 6.1051 | 6.2278 | 6.3528 | 6.4803 | 6.6101 | 6.7424 | 6.8771 | 7.4400 |
| 6 | 6.1520 | 6.3081 | 6.4684 | 6.6330 | 6.8019 | 6.9753 | 7.1533 | 7.3359 | 7.5233 | 7.7156 | 7.9129 | 8.1152 | 8.3227 | 8.5355 | 8.7537 | 8.9775 | 9.8200 |
| 7 | 7.2135 | 7.4343 | 7.6625 | 7.8983 | 8.1420 | 8.3938 | 8.6540 | 8.9228 | 9.2004 | 9.4872 | 9.7833 | 10.0889 | 10.4045 | 10.7300 | 11.0667 | 11.4144 | 12.4000 |
| 8 | 8.2857 | 8.5830 | 8.8923 | 9.2142 | 9.5491 | 9.8975 | 10.2600 | 10.6377 | 11.0218 | 11.4138 | 11.8139 | 12.2220 | 12.6393 | 13.0658 | 13.5015 | 13.9474 | 15.1000 |
| 9 | 9.3685 | 9.7546 | 10.1590 | 10.5823 | 11.0257 | 11.4891 | 11.9738 | 12.4800 | 13.0081 | 13.5590 | 14.1330 | 14.7300 | 15.3500 | 15.9930 | 16.6580 | 17.3450 | 18.8000 |
| 10 | 10.4620 | 10.9550 | 11.4640 | 12.0000 | 12.5728 | 13.1811 | 13.8160 | 14.4880 | 15.1990 | 15.9500 | 16.7420 | 17.5760 | 18.4530 | 19.3750 | 20.3430 | 21.3580 | 23.0000 |
| 11 | 11.5670 | 12.1690 | 12.8000 | 13.4680 | 14.2070 | 14.9720 | 15.7840 | 16.6450 | 17.5560 | 18.5180 | 19.5320 | 20.6000 | 21.7240 | 22.9060 | 24.1480 | 25.4520 | 27.5000 |
| 12 | 12.6830 | 13.4120 | 14.1920 | 15.0260 | 15.9170 | 16.8700 | 17.8880 | 18.9720 | 20.1240 | 21.3460 | 22.6300 | 23.9780 | 25.3930 | 26.8770 | 28.4320 | 30.0600 | 32.5000 |
| 13 | 13.8090 | 14.6800 | 15.6180 | 16.6270 | 17.7130 | 18.8820 | 20.1410 | 21.4950 | 22.9550 | 24.5230 | 26.2020 | 27.9950 | 29.9060 | 31.9380 | 34.0950 | 36.3800 | 39.5000 |
| 14 | 14.9470 | 15.9740 | 17.0960 | 18.2920 | 19.5790 | 20.9610 | 22.4420 | 24.0250 | 25.7130 | 27.5090 | 29.4160 | 31.4380 | 33.5790 | 35.8430 | 38.2340 | 40.7600 | 44.5000 |
| 15 | 16.0970 | 17.2930 | 18.5990 | 20.0240 | 21.5790 | 23.2760 | 25.1290 | 27.1520 | 29.3610 | 31.7720 | 34.4050 | 37.2800 | 40.4170 | 43.8420 | 47.5800 | 51.6600 | 56.5000 |
| 16 | 17.2580 | 18.6390 | 20.1570 | 21.8250 | 23.6570 | 25.6730 | 27.8880 | 30.3240 | 33.0030 | 35.9500 | 39.1900 | 42.7530 | 46.6720 | 50.9800 | 55.7170 | 60.9250 | 67.0000 |
| 17 | 18.4300 | 20.0120 | 21.7620 | 23.6980 | 25.8400 | 28.2130 | 30.8400 | 33.7500 | 36.9740 | 40.5450 | 44.5010 | 48.8840 | 53.7390 | 59.1180 | 65.0750 | 71.6730 | 79.0000 |
| 18 | 19.6150 | 21.4120 | 23.4140 | 25.6450 | 28.1320 | 30.9060 | 33.9990 | 37.4500 | 41.3010 | 45.5990 | 50.3960 | 55.7500 | 61.7250 | 68.3940 | 75.8360 | 84.1410 | 93.0000 |
| 19 | 20.8110 | 22.8410 | 25.1170 | 27.6710 | 30.3390 | 33.7600 | 37.3790 | 41.4460 | 46.0180 | 51.1590 | 56.9390 | 63.4400 | 70.7490 | 78.9690 | 88.2120 | 98.6030 | 108.5000 |
| 20 | 22.0190 | 24.2970 | 26.8700 | 29.7780 | 33.0660 | 36.7860 | 40.9950 | 45.7620 | 51.1600 | 57.2750 | 64.2030 | 72.0520 | 80.9470 | 91.0250 | 102.4440 | 115.3800 | 126.5000 |
| 21 | 23.2390 | 25.7830 | 28.6760 | 31.9690 | 35.7190 | 39.9930 | 44.8650 | 50.4230 | 56.7650 | 64.0020 | 72.2650 | 81.6990 | 92.4700 | 104.7680 | 118.6100 | 134.8410 | 146.5000 |
| 22 | 24.4720 | 27.2990 | 30.5370 | 34.2480 | 38.5050 | 43.3920 | 49.0060 | 55.4570 | 62.8730 | 71.4030 | 81.2140 | 92.5030 | 105.4910 | 120.4360 | 137.6320 | 157.4150 | 171.0000 |
| 23 | 25.7160 | 28.8450 | 32.4530 | 36.6180 | 41.4300 | 46.9960 | 53.4360 | 60.8930 | 69.5320 | 79.5430 | 91.1480 | 104.6030 | 120.2050 | 138.2970 | 159.2760 | 183.6010 | 200.0000 |
| 24 | 26.9730 | 30.4220 | 34.4260 | 39.0830 | 44.5020 | 50.8160 | 58.1770 | 66.7650 | 76.7900 | 88.4970 | 102.1740 | 118.1550 | 136.8310 | 158.6590 | 184.1680 | 213.9780 | 230.0000 |
| 25 | 28.2430 | 32.0300 | 36.4590 | 41.6460 | 47.7270 | 54.8650 | 63.2490 | 73.1060 | 84.7010 | 98.3470 | 114.4130 | 133.3340 | 155.6200 | 181.8710 | 212.7930 | 249.2140 | 270.0000 |
| 30 | 34.7850 | 40.5680 | 47.5750 | 56.0850 | 66.4390 | 79.0580 | 94.4610 | 113.2830 | 136.3080 | 164.4940 | 199.0210 | 241.3330 | 293.1990 | 356.7870 | 434.7450 | 530.3120 | 600.0000 |
| 35 | 41.6600 | 49.9940 | 60.4620 | 73.6520 | 90.3200 | 111.4350 | 138.2370 | 172.3170 | 216.7110 | 271.0240 | 341.5900 | 431.6830 | 546.6810 | 693.5730</ | | | |

Present Value and Future Value Tables

Table A-3 Present Value Interest Factors for One Dollar Discounted at k Percent for n Periods: $PVIF_{k,n} = 1 / (1 + k)^n$

| | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 20% | 24% | 25% | 30% |
|------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 24% | 0.9804 | 0.9709 | 0.9615 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 | 0.8621 | 0.8333 | 0.8065 | 0.8000 | 0.7692 |
| 2400 | 0.9612 | 0.9426 | 0.9246 | 0.9070 | 0.8900 | 0.8734 | 0.8573 | 0.8417 | 0.8264 | 0.8116 | 0.7972 | 0.7831 | 0.7695 | 0.7561 | 0.7432 | 0.6944 | 0.6504 | 0.6400 | 0.5917 |
| 5376 | 0.9423 | 0.9151 | 0.8890 | 0.8638 | 0.8396 | 0.8163 | 0.7938 | 0.7722 | 0.7513 | 0.7312 | 0.7118 | 0.6931 | 0.6750 | 0.6575 | 0.6407 | 0.5787 | 0.5245 | 0.5120 | 0.4552 |
| 9068 | 0.9238 | 0.8885 | 0.8548 | 0.8227 | 0.7921 | 0.7629 | 0.7350 | 0.7084 | 0.6830 | 0.6587 | 0.6355 | 0.6133 | 0.5921 | 0.5718 | 0.5523 | 0.4823 | 0.4230 | 0.4096 | 0.3501 |
| 3642 | 0.9057 | 0.8626 | 0.8219 | 0.7835 | 0.7473 | 0.7130 | 0.6806 | 0.6499 | 0.6209 | 0.5935 | 0.5674 | 0.5428 | 0.5194 | 0.4972 | 0.4761 | 0.4019 | 0.3411 | 0.3277 | 0.2693 |
| 9318 | | | | | | | | | | | | | | | | | | | |
| | 0.8880 | 0.8375 | 0.7903 | 0.7462 | 0.7050 | 0.6663 | 0.6302 | 0.5963 | 0.5645 | 0.5346 | 0.5066 | 0.4803 | 0.4556 | 0.4323 | 0.4104 | 0.3349 | 0.2751 | 0.2621 | 0.2072 |
| 3352 | 0.8706 | 0.8131 | 0.7589 | 0.7107 | 0.6651 | 0.6227 | 0.5835 | 0.5470 | 0.5132 | 0.4817 | 0.4523 | 0.4251 | 0.3996 | 0.3759 | 0.3538 | 0.2791 | 0.2218 | 0.2097 | 0.1594 |
| 5077 | 0.8535 | 0.7894 | 0.7307 | 0.6768 | 0.6274 | 0.5820 | 0.5403 | 0.5019 | 0.4665 | 0.4339 | 0.4039 | 0.3762 | 0.3506 | 0.3269 | 0.3050 | 0.2326 | 0.1789 | 0.1678 | 0.1226 |
| 5895 | 0.8368 | 0.7664 | 0.7026 | 0.6446 | 0.5919 | 0.5439 | 0.5002 | 0.4604 | 0.4241 | 0.3909 | 0.3606 | 0.3329 | 0.3075 | 0.2843 | 0.2630 | 0.1938 | 0.1443 | 0.1342 | 0.0943 |
| 3310 | 0.8203 | 0.7441 | 0.6756 | 0.6139 | 0.5584 | 0.5083 | 0.4632 | 0.4224 | 0.3855 | 0.3522 | 0.3220 | 0.2946 | 0.2697 | 0.2472 | 0.2287 | 0.1615 | 0.1164 | 0.1074 | 0.0725 |
| 944 | | | | | | | | | | | | | | | | | | | |
| | 0.8043 | 0.7224 | 0.6496 | 0.5847 | 0.5268 | 0.4751 | 0.4288 | 0.3875 | 0.3505 | 0.3173 | 0.2875 | 0.2607 | 0.2366 | 0.2149 | 0.1954 | 0.1346 | 0.0938 | 0.0859 | 0.0558 |
| 657 | 0.7885 | 0.7014 | 0.6246 | 0.5568 | 0.4970 | 0.4440 | 0.3971 | 0.3555 | 0.3188 | 0.2858 | 0.2567 | 0.2307 | 0.2076 | 0.1869 | 0.1685 | 0.1122 | 0.0757 | 0.0687 | 0.0429 |
| 218 | 0.7730 | 0.6810 | 0.6006 | 0.5303 | 0.4698 | 0.4150 | 0.3677 | 0.3262 | 0.2897 | 0.2575 | 0.2292 | 0.2042 | 0.1821 | 0.1629 | 0.1452 | 0.0935 | 0.0610 | 0.0550 | 0.0330 |
| 388 | 0.7579 | 0.6611 | 0.5775 | 0.5051 | 0.4423 | 0.3878 | 0.3405 | 0.2992 | 0.2633 | 0.2320 | 0.2046 | 0.1807 | 0.1597 | 0.1413 | 0.1252 | 0.0779 | 0.0492 | 0.0440 | 0.0254 |
| 1919 | 0.7430 | 0.6419 | 0.5553 | 0.4810 | 0.4173 | 0.3624 | 0.3152 | 0.2745 | 0.2394 | 0.2090 | 0.1827 | 0.1599 | 0.1401 | 0.1229 | 0.1079 | 0.0649 | 0.0397 | 0.0352 | 0.0195 |
| 96 | | | | | | | | | | | | | | | | | | | |
| | 0.7284 | 0.6232 | 0.5339 | 0.4581 | 0.3936 | 0.3387 | 0.2919 | 0.2519 | 0.2176 | 0.1883 | 0.1631 | 0.1415 | 0.1229 | 0.1069 | 0.0930 | 0.0541 | 0.0320 | 0.0281 | 0.0150 |
| 443 | 0.7142 | 0.6050 | 0.5134 | 0.4363 | 0.3714 | 0.3166 | 0.2703 | 0.2311 | 0.1978 | 0.1686 | 0.1456 | 0.1252 | 0.1078 | 0.0929 | 0.0802 | 0.0451 | 0.0258 | 0.0225 | 0.0115 |
| 41 | 0.7002 | 0.5874 | 0.4936 | 0.4155 | 0.3503 | 0.2959 | 0.2502 | 0.2120 | 0.1799 | 0.1528 | 0.1300 | 0.1108 | 0.0946 | 0.0800 | 0.0691 | 0.0376 | 0.0208 | 0.0180 | 0.0089 |
| 39 | 0.6864 | 0.5703 | 0.4746 | 0.3957 | 0.3305 | 0.2765 | 0.2317 | 0.1945 | 0.1635 | 0.1377 | 0.1161 | 0.0981 | 0.0829 | 0.0703 | 0.0596 | 0.0313 | 0.0168 | 0.0144 | 0.0068 |
| 58 | 0.6730 | 0.5537 | 0.4564 | 0.3769 | 0.3118 | 0.2584 | 0.2145 | 0.1784 | 0.1486 | 0.1240 | 0.1037 | 0.0868 | 0.0728 | 0.0611 | 0.0514 | 0.0261 | 0.0135 | 0.0115 | 0.0053 |
| 64 | | | | | | | | | | | | | | | | | | | |
| | 0.6598 | 0.5375 | 0.4388 | 0.3589 | 0.2942 | 0.2415 | 0.1987 | 0.1637 | 0.1351 | 0.1117 | 0.0926 | 0.0768 | 0.0638 | 0.0531 | 0.0443 | 0.0217 | 0.0109 | 0.0092 | 0.0040 |
| 32 | 0.6468 | 0.5219 | 0.4220 | 0.3418 | 0.2775 | 0.2257 | 0.1839 | 0.1502 | 0.1228 | 0.1007 | 0.0826 | 0.0680 | 0.0560 | 0.0462 | 0.0382 | 0.0181 | 0.0088 | 0.0074 | 0.0031 |
| 74 | 0.6342 | 0.5067 | 0.4057 | 0.3256 | 0.2618 | 0.2109 | 0.1703 | 0.1378 | 0.1117 | 0.0907 | 0.0738 | 0.0601 | 0.0491 | 0.0402 | 0.0329 | 0.0151 | 0.0071 | 0.0059 | 0.0024 |
| 31 | 0.6217 | 0.4919 | 0.3901 | 0.3101 | 0.2470 | 0.1971 | 0.1577 | 0.1264 | 0.1015 | 0.0817 | 0.0659 | 0.0532 | 0.0431 | 0.0349 | 0.0284 | 0.0126 | 0.0057 | 0.0047 | 0.0018 |
| 31 | 0.6095 | 0.4776 | 0.3751 | 0.2953 | 0.2330 | 0.1842 | 0.1460 | 0.1160 | 0.0923 | 0.0736 | 0.0588 | 0.0471 | 0.0378 | 0.0304 | 0.0245 | 0.0105 | 0.0046 | 0.0038 | 0.0014 |
| 12 | | | | | | | | | | | | | | | | | | | |
| | 0.5521 | 0.4120 | 0.3083 | 0.2314 | 0.1741 | 0.1314 | 0.0994 | 0.0754 | 0.0573 | 0.0437 | 0.0334 | 0.0256 | 0.0196 | 0.0151 | 0.0116 | 0.0042 | 0.0016 | 0.0012 | * |
| 20 | 0.5000 | 0.3554 | 0.2534 | 0.1813 | 0.1301 | 0.0937 | 0.0676 | 0.0490 | 0.0356 | 0.0259 | 0.0189 | 0.0139 | 0.0102 | 0.0075 | 0.0055 | 0.0017 | 0.0005 | * | * |
| 1 | 0.4902 | 0.3450 | 0.2437 | 0.1727 | 0.1227 | 0.0875 | 0.0626 | 0.0449 | 0.0323 | 0.0234 | 0.0169 | 0.0123 | 0.0089 | 0.0065 | 0.0049 | 0.0014 | * | * | * |
| 1 | 0.4529 | 0.3066 | 0.2083 | 0.1420 | 0.0972 | 0.0668 | 0.0460 | 0.0318 | 0.0221 | 0.0154 | 0.0107 | 0.0075 | 0.0053 | 0.0037 | 0.0026 | 0.0007 | * | * | * |
| 8 | 0.3715 | 0.2281 | 0.1407 | 0.0872 | 0.0543 | 0.0339 | 0.0213 | 0.0134 | 0.0085 | 0.0054 | 0.0035 | 0.0022 | 0.0014 | 0.0009 | 0.0006 | * | * | * | * |

Table A-4 Present Value Interest Factors for a One-Dollar Annuity Discounted at k Percent for n Periods: $PVIFA = [1 - 1/(1 + k)^n] / k$

| | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 20% | 24% | 25% | 30% |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1 | 0.9804 | 0.9709 | 0.9615 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 | 0.8621 | 0.8333 | 0.8065 | 0.8000 | 0.7692 |
| 4 | 1.9416 | 1.9135 | 1.8861 | 1.8594 | 1.8334 | 1.8080 | 1.7833 | 1.7591 | 1.7355 | 1.7125 | 1.6901 | 1.6681 | 1.6467 | 1.6257 | 1.6052 | 1.5278 | 1.4568 | 1.4400 | 1.3609 |
| 8 | 2.8639 | 2.8286 | 2.7751 | 2.7232 | 2.6730 | 2.6243 | 2.5771 | 2.5313 | 2.4869 | 2.4437 | 2.4018 | 2.3612 | 2.3216 | 2.2832 | 2.2459 | 2.1065 | 1.9813 | 1.9520 | 1.8161 |
| 12 | 3.8077 | 3.7171 | 3.6299 | 3.5460 | 3.4651 | 3.3872 | 3.3121 | 3.2397 | 3.1699 | 3.1024 | 3.0373 | 2.9745 | 2.9137 | 2.8550 | 2.7982 | 2.5887 | 2.4043 | 2.3616 | 2.1662 |
| 16 | 4.7135 | 4.5797 | 4.4518 | 4.3295 | 4.2124 | 4.1002 | 3.9927 | 3.8897 | 3.7908 | 3.6959 | 3.6048 | 3.5172 | 3.4331 | 3.3522 | 3.2743 | 2.9906 | 2.7454 | 2.6893 | 2.4356 |
| 20 | 5.6014 | 5.4172 | 5.2421 | 5.0757 | 4.9173 | 4.7665 | 4.6229 | 4.4859 | 4.3553 | 4.2305 | 4.1114 | 3.9975 | 3.8887 | 3.7845 | 3.6847 | 3.3255 | 3.0205 | 2.9514 | 2.6427 |
| 24 | 6.4720 | 6.2303 | 6.0021 | 5.7864 | 5.5824 | 5.3893 | 5.2064 | 5.0330 | 4.8694 | 4.7122 | 4.5638 | 4.4226 | 4.2883 | 4.1604 | 4.0386 | 3.6046 | 3.2423 | 3.1611 | 2.8021 |
| 28 | 7.3255 | 7.0197 | 6.7327 | 6.4632 | 6.2098 | 5.9713 | 5.7466 | 5.5348 | 5.3349 | 5.1461 | 4.9676 | 4.7988 | 4.6389 | 4.4873 | 4.3436 | 3.8372 | 3.4212 | 3.3289 | 2.9247 |
| 32 | 8.1622 | 7.7861 | 7.4353 | 7.1078 | 6.8017 | 6.5162 | 6.2469 | 5.9952 | 5.7590 | 5.5370 | 5.3282 | 5.1317 | 4.9464 | 4.7716 | 4.6065 | 4.0310 | 3.5655 | 3.4631 | 3.0190 |
| 36 | 8.9826 | 8.5302 | 8.1109 | 7.7217 | 7.3601 | 7.0236 | 6.7101 | 6.4177 | 6.1446 | 5.8892 | 5.6502 | 5.4262 | 5.2161 | 5.0188 | 4.8332 | 4.1925 | 3.6819 | 3.5705 | 3.0915 |
| 40 | 9.7868 | 9.2526 | 8.7505 | 8.3064 | 7.8869 | 7.4987 | 7.1390 | 6.8052 | 6.4951 | 6.2085 | 5.9377 | 5.6869 | 5.4527 | 5.2337 | 5.0286 | 4.3271 | 3.7757 | 3.6564 | 3.1473 |
| 44 | 10.5755 | 9.9540 | 9.3851 | 8.8633 | 8.3838 | 7.9427 | 7.5361 | 7.1607 | 6.8137 | 6.4924 | 6.1944 | 5.9176 | 5.6603 | 5.4206 | 5.1971 | 4.4392 | 3.8514 | 3.7251 | 3.1903 |
| 48 | 11.3448 | 10.6355 | 9.9856 | 9.3936 | 8.8527 | 8.3577 | 7.9038 | 7.4869 | 7.1034 | 6.7499 | 6.4235 | 6.1218 | 5.8424 | 5.5831 | 5.3423 | 4.5327 | 3.9124 | 3.7801 | 3.2233 |
| 52 | 12.1061 | 11.2961 | 10.5633 | 9.8986 | 9.2950 | 8.7455 | 8.2442 | 7.7862 | 7.3687 | 6.9819 | 6.6282 | 6.3025 | 6.0021 | 5.7245 | 5.4675 | 4.6106 | 3.9616 | 3.8241 | 3.2487 |
| 56 | 12.8491 | 11.9338 | 11.1181 | 10.3801 | 9.7122 | 9.1079 | 8.5595 | 8.0607 | 7.6081 | 7.1909 | 6.8109 | 6.4624 | 6.1422 | 5.8474 | 5.5755 | 4.6755 | 4.0013 | 3.8593 | 3.2682 |
| 60 | 13.5781 | 12.5611 | 11.8521 | 11.1038 | 10.4066 | 9.7665 | 9.1854 | 8.6526 | 8.1612 | 7.7092 | 7.2972 | 6.9169 | 6.5683 | 6.2511 | 5.9542 | 5.0286 | 4.3333 | 4.1874 | 3.5832 |
| 64 | 14.2921 | 13.1666 | 12.4666 | 11.7274 | 11.0477 | 10.4273 | 9.8562 | 9.3346 | 8.8533 | 8.4071 | 7.9916 | 7.6039 | 7.2479 | 6.9219 | 6.6172 | 5.6748 | 4.9591 | 4.8099 | 4.2048 |
| 68 | 14.9921 | 13.7544 | 13.0559 | 12.2859 | 11.6090 | 10.9828 | 10.4019 | 9.8607 | 9.3594 | 8.8924 | 8.4549 | 8.0439 | 7.6549 | 7.2959 | 6.9587 | 5.9987 | 5.2748 | 5.1199 | 4.5097 |
| 72 | 15.6781 | 14.3244 | 13.6244 | 12.8185 | 12.1158 | 11.4885 | 10.9036 | 10.3581 | 9.8479 | 9.3669 | 8.9119 | 8.4883 | 8.0939 | 7.7299 | 7.3927 | 6.4187 | 5.6935 | 5.5297 | 4.9150 |
| 76 | 16.3511 | 14.8777 | 14.1799 | 13.3462 | 12.6047 | 11.9547 | 11.3562 | 10.7969 | 10.2739 | 9.7819 | 9.3189 | 8.8819 | 8.4683 | 8.0827 | 7.7247 | 6.7307 | 6.0055 | 5.8317 | 5.2162 |
| 80 | 17.0111 | 15.4151 | 14.7199 | 13.8621 | 13.1666 | 12.5666 | 11.9666 | 11.4033 | 10.8733 | 10.3733 | 9.9019 | 9.4569 | 9.0369 | 8.6407 | 8.2767 | 7.2707 | 6.5455 | 6.3617 | 5.7452 |
| 84 | 17.6581 | 15.9377 | 15.2451 | 14.4511 | 13.7042 | 1 | | | | | | | | | | | | | |