## EASTERN UNIVERSITY, SRI LANKA

## FACULTY OF COMMERCE AND MANAGEMENT

Har First Semester Examination in Bachelor of Commerce (Specialization wunting and Finance) / Bachelor of Commerce (Specialization in Business Economics)-2016/2017(January 2019) (Proper/Repeat)

DAF 4043 Portfolio Investment Analysis

All Questions
Time Allowed: 03 Hours
gorammable Calculator and Time Value Tables are permitted.

Define the term "Portfolio Investment".
(05 Marks)
Brifly describe the role of financial intermediaries in mobilizing funds for ivestments.
(05 Marks)
Briefly explain the investment management process.
(05 Marks)

Explain the types of investment.
(05 Marks)
Explain how an individual investor draft his/her investment policy.
(05 Marks)
02. (I) Suppose If two assets, $P$ and $Q$, are said to have expected returns of 12 in $18 \%$ and standard deviations of returns of $6 \%$ and $10 \%$ respectively. Whicha shall be selected for investment based on Coefficient of Variation of returns?
(II) Calculate the Expected Rate of Return and the Standard Deviation of the Res for an asset which has the following possible returns with associated probabili

| Probabilities | Possible Returns (\%) |
| :---: | :---: |
| 0.35 | 21 |
| 0.15 | 11 |
| 0.25 | 19 |
| 0.20 | -05 |
| 0.05 | 13 |

(III) Securities A, B and C have the following characteristics:

| Probability | Possible Return (\%) |  |  |
| :---: | :---: | :---: | :---: |
|  | Security A | Security B | Security C |
| 0.25 | -15 | 05 | 08 |
| 0.20 | 05 | 15 | 05 |
| 0.30 | 40 | -10 | 02 |
| 0.25 | -10 | 10 | 05 |

## Required:

Calculate the following:
(a) The Co-Variance between returns of the Securities.
(b) The Correlation Coefficients between returns of the Securities
(c) The Expected Rate of Return and the Standard deviation of the returns the portfolio of securities $\mathrm{A}, \mathrm{B}$ and C , combined in the proportion of 4 respectively.
lecording to the Capital Assets Pricing Model (CAPM) what would the erpected return of an investment having a Beta of 2.50 , If the risk-free rate of mumn is $5 \%$ and the return on the market portfolio is $15 \%$.

Using hypothetical figures for the measurement of Expected Return and the Risk for three portfolio investments, explain how an investor choose among portfolios as explained by the Markowitz portfolio theory.

In Investor owns a portfolio of four securities. The characteristics of the securities an their amounts invested in the portfolio are presented below.

| Security | Beta | Amount <br> invested <br> (Rs.000) | Expected <br> Return (\%) |
| :---: | :---: | :---: | :---: |
| A | 2.60 | 3500 | 22 |
| B | 0.90 | 2500 | 15 |
| C | 1.00 | 1500 | 11 |
| D | -1.50 | 2500 | 17 |

Required:
(a). What is the expected rate of return of this portfolio?
(b) What is the risk of the portfolio?
(c) What would be your recommendation for the investor if he/she wants to reduce the risk in the portfolio?
04. (I) The following are the annual returns of a security of PST plc and the market (M) the last five years

| Year | Returns (\%) |  |
| :---: | :---: | :---: |
|  | PST | $M$ |
| 2014 | 12 | 15 |
| 2015 | 15 | 20 |
| 2016 | -05 | -02 |
| 2017 | 10 | 14 |
| 2018 | -08 | -05 |

Required:
(i) Calculate the beta coefficient for the security of PST plc.
(ii) Find (a) Total Risk, (b) Systematic Risk, and (c) Unsystematic Risk of security of PST plc.
(II) An investor holds an investment on the bonds of the CRM plc having a parvai of Rs. 1000 each with coupon rate of $14 \%$ per annum payable semi annuallys the maturity of 10 years.
(i) Explain the impact of changes in the market interest rates on the valua bonds.
(ii) What will be the value of the bond of the CRM plc if the market inter: rate increases to $16 \%$ at the end of two year?
(iii) What will be the value of the bond of the CRM plc if the market inter rate decreases to $12 \%$ at the end of six years?
(iv) If the value of the bond of the CRM plc is Rs. 1500 at the time the bohas two year remaining maturity, what would be the YTM of the bond?

Table A-3 Present Value interest Factors for One Dollar Discounted at $k$ Percent for $n$ Periods: PViF $k, n=1 /(1+k)^{n}$

|  | 5 | 28 | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% | $\frac{16 \%}{0.8621}$ | 20\% 83 | 24'1/4 | 0.8000 | 0.7692 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 13 | 09709 | 0.8645 | 0.9624 | 0.9434 | 0.9346 | 0.9259 | 0.8174 | 0.9091 | 0.9009 | 0.8929 | 0.6880 | 0.8772 | 0.8686 | 0.7432 | 0.6944 | 0.5804 | 0.6400 | 0.5947 |
|  | 1412 | 09426 | 0.9246 | 0.9070 | 0.8900 | 0.8734 | 0.8573 | 0.8417 | 0.8264 | 0.8116 | 0.7972 | 0.6931 | 0.6750 | 0.6576 | 0.6407 | 0.5787 | 0.5245 | 0.5120 | 0.4562 |
|  | U4\% | 0.9151 | 0.8890 | 0.8638 | 0.8336 | 0.8163 | 0.7938 | 0.7722 | 0.7513 | 0.7312 | 0.6355 | 0.6133 | 0.6321 | 0.5718 | 0.5523 | 0.4823 | 0.42:30 | 0.4096 | 0.3501 |
|  | uni | 0:3855 | 0.8548 | 0.8227 | 0.7921 | 0.7629 | 0.7350 | 0.7084 | 0.6830 | 0.5935 | 0.5674 | 0.6428 | 0.519 .4 | 0.4972 | 0.4761 | 0.4019 | 0.3411 | 0.3277 | 0.2693 |
|  | Lum | 0.8626 | 0.8219 | 0.7835 | 0.7473 | 0.7130 | 0.6806 | 0.6499 |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  | 0.53 .46 | 0.5066 | 0.4803 | 0.4556 | 0.4323 | 0.4104 | 0.3349 | 0.2751 | 0.2621 | . 2072 |
|  | $13 \% 0$ | 0.8375 | 0.7903 | 0.7462 | 0.7050 | 0.5663 | 0.6302 |  | 0.5132 | 0.4817 | 0.4523 | 0.4251 | 0.3996 | 0.3759 | 0.3538 | 0.2791 | $0.2 \times 18$ | 0.2097 | 0.1684 |
|  | U\% | 0.8131 | 0.7699 | 0.7107 | 0.6655 | 0.6227 | 0.5635 | . 64 |  | . 4339 | 0.4039 | 0.3762 | 0.3506 | 0.3269 | 0.3050 | 0.2326 | 0.1789 | 0.1678 | 0.1226 |
|  | 1535 | 0.769 | 0.7307 | 0.6768 | 0.6274 | 0.5820 |  | 0.4604 | 24 | 0.3909 | 0.3806 | 0.3329 | 0.3075 | 0.2843 | 0.2630 | 0.1938 | 0.1443 | 0.1342 | 0.0943 |
|  | 123 | 0.7654 | 0.7026 | 0.6445 | 0.5 | 0.5439 | 0.5002 | 4224 | 0.3855 | 0.3522 | 0.3220 | 0.2946 | 0.2697 | 0.2472 | 0.2267 | 0.1515 | 0.1164 | 0.1074 | 0.0725 |
|  | UM | 0.7441 | 0.6756 | 0.6139 | 0.5584 | 0.5083 | 0.4632 | 4224 |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 0.3505 | 0.3173 | 0.2876 | 0.2607 | 0.2366 | 0.2149 | 0.1954 | 0.1346 | 0.0938 | 0.0859 | 0.9558 |
| x | H04 | 0.7224 | 0.6496 | 0.5847 | 0.5268 | 0. |  | 3555 | 0.3186 | 0.2858 | 0.2557 | 0.2307 | 0.2676 | 0.1869 | 0.4685 | 0.1122 | 0.0757 | 0.0687 | 0.0429 |
| in | LTMS | 0.7014 | 0.6248 | 0.5588 | 0.4970 | 0.4440 | 0.3971 | 3262 | 0.2897 | 0.2575 | 0.2292 | 0.2042 | 0.1821 | 0.1625 | 0.1452 | 0.0935 | 0.0610 | 0.0550 | 0.0330 |
| (6) | 1730 | 0.6510 | 0.5006 | 0.6303 | 0.4688 | 0.4160 | 0.3677 |  | 0.2633 | 0.2320 | 0.2046 | 0.1807 | 0.1597 | 0.1413 | 0.1252 | 0.0779 | 0.0492 | 0.0440 | 0.0254 |
| m | 1527 | 0.6611 | 0.5775 | 0.5051 | 0.4423 | 0.3878 | 0.3405 |  | 0.2 | 0.2090 | 0.9827 | 0.1599 | 0.1401 | 0.1328 | 0.1079 | 0.0649 | 0.0397 | 0.0362 | 0.0195 |
| n | 1740 | 0.6419 | 0.5553 | 0.4810 | 0.4173 | 0.3624 | 0.3152 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 0.2176 | 0.188 | 0.1631 | 0.1415 | 0.9229 | 0.1069 | 0.0930 | 0.0541 | 0.0320 | 0.0281 | 0.0160 |
| (13) | 2234 | 0.6232 | 0.5339 | 0.4581 | 0.3936 | 0.3387 | 0.2 |  | 0.1978 | 0.16 | 0.1456 | 0.1252 | 0.1078 | 0.0929 | 0.0802 | 0.0451 | 0.0258 | 0.0225 | 0.0116 |
| $\pm$ | Q2142 | 0.5050 | 0.5134 | 0.4363 | 0.3714 | 0.3466 | 0.2703 |  | 0.1799 | 0.1528 | 0.1300 | 0.7708 | 0.0946 | 0.0808 | 0.0691 | 0.0376 | 6.0208 | 0.0180 | 0.0089 |
| 128 | 2002 | 0.5874 | 0.4936 | 0.4155 | 0.3603 | 0.2959 | 0.2502 |  | 0.1635 | 0.1377 | 0.1164 | 0.0887 | 0.0829 | 0.0703 | 0.0596 | 0.0313 | 0.0158 | 0.0144 | 0.0088 |
| It | 124 | 0.5703 | 0.4746 | 0.3967 | 0.3305 | 0.2785 | 0.2317 | 178 | 0.1486 | 0.1240 | 0.1037 | 0.0868 | 0.0728 | 0.0611 | 0.0514 | 0.0261 | 0.0135 | 0.0115 | 0.0053 |
| 34 | 1972 | 0.5537 | 0.4564 | 0.3769 | 0.3118 | 0.2634 | 0.2145 | .1784 |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 0.4637 | 0.1351 | 0.1117 | 0.0926 | 0.0768 | 0.0638 | 0.0631 | 0.0443 | 0.0217 | 0.0109 | 0.0092 | 0.0040 |
| I4 | 1355 | 0.5375 | 0.4388 | 0.3589 | 0.2942 | 0.2415 | 0.1987 |  | 0.12 .28 | 0.1007 | 0.18826 | 0.0680 | 0.0560 | 0.0462 | 0.0382 | 0.0181 | 0.0088 | 0.0074 | 0.0031 |
| - | 1345 | 0.5219 | 0.4220 | 0.3418 | 0.2775 | 0.2257 | 0.1839 |  | 18 | 0.0807 | 0.0738 | 0.0881 | 0.0491 | 0.0402 | 0.0329 | 0.0151 | 0.0071 | 0.0059 | 0.0024 |
| 13 | 6342 | 0.5067 | 0.4057 | 0.3256 | 0.2818 | 0.2109 | 0.1703 |  |  | 0.0817 | 0.0659 | 0.0532 | 0.0431 | 0.0349 | 0.0284 | 0.0126 | 0.0057 | 0.0047 | 0.0048 |
| 18 | 05217 | 0.4919 | 0.3901 | 0.3101 | 0.2470 | 0.1971 | 0.1577 |  | 3 | 0.0736 | 0,0688 | 0.0471 | 0.0378 | 0.0304 | 0.0245 | 0.0105 | 0.0046 | 0.0038 | 0.0014 |
| 71 | 0.605 | 0.4776 | 0.3751 | 0.2953 | 0.2330 | 0.1842 | 0.1460 | 0.1160 |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | 0.0573 | 0.0437 | 0.0334 | 0.0265 | 0.0196 | 0.0151 | 0.0176 | 0.0042 | 0.0016 | 0.0012 | * |
| (1) | 05521 | 0.4120 | 0.3083 | 0.2314 | 0.1741 |  |  |  | 0.0356 | 0.7259 | 0.0189 | 0.0139 | 0.0102 | 0.0075 | 0.0055 | 0.0017 | 0.0005 | $\stackrel{ }{ }$ | * |
| 318 | 0.5000 | 0.3654 | 0.2634 | 0.1813 | 0.1301 | 37 |  |  | 0.0323 | 0.0234 | 0.0169 | 0.0123 | 0.0039 | 0.0065 | 0.0048 | 0.0014 | - | * | $\cdot$ |
| 117 | 0.492 | 0.3450 | 0.2437 | 0.4727 | 0.1227 | 0.0875 |  | 0.0318 | 0.0221 | 0.0154 | 0.0107 | 0.0075 | 0.0053 | 0.0037 | 0.0026 | 0.0007 | * | - | $\bullet$ |
|  |  |  |  | 0.1420 | 0.0972 | 0.0668 | 0.0460 | 0.0318 |  |  |  |  |  |  | 006 | * |  | * | - |



Table A-4 Present Value Interest Factors for a One-Dollar Amnuity Discounted at $k$ Percent for $n$ Periods: PVIFA $\left.=[1-1 / 41+k)^{n}\right] / k$

 | 1. 196 | 31.424 | 25.730 |
| :--- | :--- | :--- |

Table A-1 Future Value interest Factors for One Dollar Compounded at $k$ Percent for $n$ Periods: $F V F_{h}=(1+k)^{\prime}$

| Period | 1\% | 2\% | 3\% | 4\% | 6\% | 8\% | 7\% | 8\% | 9\% | 10\% | \$1\% | 12\% | 13\% |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.0100 | 1.0200 | 1.0300 | 1.0400 | 1.0500 | 1. 0600 | 1.0\%00 | 1.0800 | 1.0900 | 1.1100 | 1.1100 | 1.1200 | 1.1350 | 1.1400 | ${ }_{1}^{15 \%}$ | 10\% | W | $\frac{4}{4}$ |
| 2 | 1.0201 | 1.0404 | 1.0808 | 1.8816 | 1.1025 | ¢.1236 | 1.1449 | 1.1664 | 1.1881 | 1.2100 | 1.2321 | 1.1200 | 1.12760 | 1.1400 | 1,1600 | 1.1600 | 1.2 m |  |
| 3 | 1.0303 | 1.0612 | 1.0927 | 1.1248 | 1.1576 | 1.1910 | 1.22 | 1.25 |  | 1.3310 | 3675 | 1.2544 | 1.2769 | 1.2996 | 1.3225 | 1.3056 | uma |  |
| 4 | 1.0406 | 1.0824 | 1.1255 | 1.1699 | 4.2155 | 1.262 | 4.3.108 | 1.3605 | 1.4116 | 1.46:4 | 1.3672 | 1.4049 | 1.4429 | 1.4816 | 1.5200 | 1.5609 | 1200 | H |
| 5 | 1.0510 | 1.1041 | 1.1693 | 1.2167 | 1,2763 | 1.3332 | 1.41126 | 1.4693 | 1.5386 |  | ${ }^{1.66851}$ |  | \% 6305 | 1.6890 | 1.7490 | 1.8106 | 2078 |  |
|  |  |  |  |  |  |  |  |  |  |  | 1.6857 | 1.7623 | 1.8424 | 1.9254 | 2.0114 | 2.1003 | 20n | m |
| 6 | 1.0615 | \$.1262 | \$.1941 | 1.2653 | 1.3401 | 1.4185 | 1.6007 | 1.5869 | 1.1877 | 1.7746 |  |  |  |  |  |  |  |  |
| 7 | 1.0721 | 1.1487 | 1.2299 | 1.3159 | 1.4071 | 1.5036 | 1.51758 | 1.7138 | 1.8280 | $\frac{1.7716}{1.9487}$ | 2.0762 |  | 2.08:0 | 2.1950 | 2.3131 | 2.4364 | 290 | $1 \times$ |
| 8 | 1.0829 | 1.1717 | 1.2668 | 1.3586 | 1.4776 | 1.5938 | 1.7182 | 1.850 | 1.9926 | 2.4436 | 2.3045 | 2.4760 | ${ }^{3658.6}$ | 2.5023 | 2.6600 | 2.8262 | \%m | 1 |
| 9 | 1.9937 | 1.1951 | 1.3043 | 1.4233 | 1.6513 | 1.6895 | 1.8385 | 1.9990 | 2.1719 | 2.3579 | 2.6580 | 2.7731 | 2.6564 | 2.8526 | 3.0590 | 3.274 | 438 | 13 |
| 10 | 1.1046 | 1.2490 | 1.3439 | 1.4802 | 1.6289 | 1.7908 | 1.9672 | 2.1589 | 2.3674 | 2.693 |  |  | 3.0040 | 3.2519 | 3.5179 | 8030 | 5.15\% |  |
|  |  |  |  |  |  |  |  |  |  | 2.6837 | 2.8394 | 3.10 | 3.3946 | 707 | 4.0456 | 4.414 | 6.171 | His |
| 11 | 1.1157 | 1.2434 | 1.3842 | 1.5395 | 1.7103 | 1.8983 | 2.1049 | 2,3316 | 2.58 | 2.9534 | 3.159a | 3.4786 |  |  |  |  |  |  |
| 12 | 1.1268 | 1.2682 | 1.4258 | 1.6010 | 1.7959 | 2.0122 | 2.2522 | 2.5182 | 2.8127 | 3.1384 | 3.4985 | 3.47 | 3,8369 | . 8282 | 4.6624 | 5.1773 | tam | 4 |
| 13 | 1.1381 | 1.2936 | 1.4585 | 1.6651 | 1.8855 | 2.1329 | 2.4098 | 2.7496 | 3.0658 | 3.4623 | 3.8833 | 4.3635 | 4.80410 | 4.8179 | 6.3503 | 6.9360 | ¢. 115 | 41 |
| 14 | +1495 | +.3196 | 1.5126 | 1.7317 | 1.9799 | 2.2609 | 2.5785 | 2.9372 | 3417 | 3.7875 | 4.31 | 4.387\% | 5.56348 | 6.4924 | 6,1628 | 6.8868 | 10.50 | 4 |
| 16 | 1.1610 | 1.3469 | 1.6550 | 1.8009 | 2.0789 | 2.3965 | 2.7590 | 3.1722 | 3.6425 | 4.1772 | 4.7846 | 5.473 | 6.2563 |  |  | 9875 | 1203 | 11 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 371 | 9.2655 | 1245 | 47 |
| 15 | 1.1726 | ¢ 7.3728 | 1.6047 | 8730 | 2.1829 | 2.5404 | 2.9122 | 3.4259 | 3.9703 | 4.5950 |  |  |  |  |  |  |  |  |
| 17 | 1.1843 | 1.4002 | 528 | 1.9479 | 2.2920 | 2.6928 | 3.1688 | 3.7000 |  |  |  |  | 7.0673 | . 1372 | 9.367 | 10.748 | 宸 | Hx |
| 18 | 1.1969 | 1.4282 | 1.7024 | 2.0258 | 2.4066 | 2.8543 | 3.379 | 3.9960 | 4.37171 | S4, | 5.8964 | 6.8660 | 7.9864 | 9.2765 | 10.761 | 12.468 | 21.15 | 48 |
| 19 | 1.2081 | 1.4568 | 1.7 | 2.1068 | 2.5270 | 3.0256 | 3.6165 | 4.3157 | 5.1417 |  |  |  | 3.0243 | 0.675 | 12.375 | 14.463 | 24.53 | 413 |
| 20 | 7.2202 | 1.4859 | 1.8061 | 2.1941 | 2.8533 | 3.2071 | 3.81697 | 4.6610 | 044 | 375 | ${ }^{7.2633}$ | 8.6128 | 10.997 | 12.056 | 14.232 | 16.777 | 3154 | 1 H |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | 3.743 | 86.387 | 19,461 | 3138 | 15 |
| 21 | 1.2324 | 1.5157 | 1.8603 | 2.2788 | 2.7860 | 3.3996 | 4.1406 | 5.0338 | 8. 4088 | 7.4002 |  |  |  |  |  |  |  |  |
| 22 | 1.2447 | 1.5480 | 1.9161 | 2.3699 | 2.9263 | 3.6036 | 4.4304 | 5.4385 | 6.6586 | 8.1403 | ${ }^{\text {6,9492 }}$ |  |  |  | -12.822 | 22.574 | 4 \%00s | NH |
| 23 | 2572 | 5769 | . 9736 | 2.4647 | 3.0715 | 3.8197 | 4.7405 | 6.8715 | 7.257 |  |  |  |  |  | 21.645 | 26.186 | 55201 | 140 |
| 24 | 4.2697 | 1.6084 | 2.0328 | 2.5633 | 3.2251 | 4.0489 | 5.0724 | 6.3412 | 7.9141 | 9.8497 | 12.239 | 15.179 |  | 20.362 | 24.891 | 30.376 | 6624 | 142 |
| 25 | 1.2824 | 1.8406 | 2.0938 | 2.6658 | 3.3664 | 4.2919 | 6.4.274 | 6.8465 | 8.6231 | 10.335 | 13.585 | 17,000 | 21.234 | 26.462 | 32.919 | ${ }_{4}^{35.23674}$ | 97 | ne |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 30 | 1.3478 | 1.81114 | 2,4273 | 3.2434 | 4.3218 | 5.7435 | 7.6123 | 10.063 | 13.268 | 17.149 | 22.a92 | 29.960 | 39.116 | 50.950 | 66.212 |  |  |  |
| 35 | 1.4166 | 1.9999 | 2.8139 | 3.9461 | 5.5160 | 7.6861 | 10.677 | 14.785 | 20.414 | 28.402 | 38.575 | 52.800 | 72.069 | 98.100 | 133.176 | 18.314 | 2720 |  |
| 36 40 | 1.4308 | 2.0399 | 2.8983 | 4.1039 | 8.7918 | 8.1473 | 14.424 | 15.968 | 22.251 | 30.913 | 42.818 | 59.136 | 81.437 | 119.834 | 153.952 | 209.154 | 500. |  |
| 50 | 1.48889 | 2.2080 | 3.2620 | 4.8010 | 7.0400 | 10.288 | 14,374 | 21.725 | 31.409 | 45.359 | 65.001 | 93.051 | 132.782 | 188.984 | 267.864 | 378.721 |  |  |
|  |  | 2.6996 | 4.3838 | 067 | 11.467 | 18.420 | 29.457 | 46.902 | 74.358 | 117.391 | 184.565 | 289.002 | 450.738 | 700.233 | . |  |  |  |

Table A-2' Future Value interest Factors for a One-Dollar Annuity Compouned at $k$ Percent for $n$ Periods: $F V / F A_{k n}=\left[(1+k)^{k}-1\right] / 1$

| Period | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 9\% | 9\% |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\ddagger$ | 1.0000 | 1.0200 | 1.03300 | 1.0400 | 1.0500 | 1.0600 | 1.0700 | 1.0800 | 1.0900 | 1.1000 | 111100 | 12\% | 13\% | 14\% | 15\% | 16\% | 20\% | 41 |
| 2 | 2.0100 | 2.0200 | 2.0300 | 2.0400 | 2.0500 | 2.0600 | 2.0700 | 2.0800 | 2.0800 | 2.11000 | 2.1100 |  | 1.13100 | 1.1400 | 1.1500 | 1.1800 | 1.200 | 13 |
| 3 | 3.0301 | 3.0604 | 3.0909 | 3.1216 | 3.1525 | 3.1836 | 3.2149 | 3.2464 | 3.2781 | 3.3.160 | 2.1700 | 2.1200 | 2.1300 | 2.1400 | 2.1600 | 2.1600 | 2.2000 | 2 |
| 4 | 4.0604 | 4.1216 | 4.1836 | 4.2465 | 4.3101 | 4.3746 | 4.4399 | 4.5061 | 4.5731 | 4.6410 | 3.3421 | 3.3744 | 3.4069 | 3.4386 | 3.4725 | 3.5058 | 3.6600 | 17 |
| 5 | 5.1010 | 5.2040 | 5.3091 | 5.4163 | 5.5256 | 5.6371 | 5.7507 | 5.8866 | 8.9847 |  | 4.7097 | 4.7793 | 4.84!38 | 4.9211 | 4.9934 | 6.0865 | 5.360 |  |
|  |  |  |  |  |  |  |  |  | 8.0047 | 6.1069 | 5.2278 | 6.3623 | 6.4818 | 6.6101 | 6.7424 | 6.8771 | 7.441 | 1 |
| 6 | 6.1520 | 6.3081 | 6.4684 | 6.6330 | 6.8019 | 6.9753 | 7.1533 | 7.3359 | 7.5233 |  |  |  |  |  |  |  |  |  |
| 7 | 7.2135 | 7.4343 | 7.6625 | 7.8933 | 8.1420 | 8.3938 | 8.6540 | 2.9228 | 9.2004 |  |  |  |  | 8.5355 | 8.7537 | 8.8775 | 9.92919 | 14 |
| 8 | 8.2857 | 8.5830 | 8.8923 | 9.2142 | 9.5491 | 9.6975 | 40.260 | 10.637 | 11.028 |  |  | 0.08 | 10.4 | 10.730 | 11.067 | 11.414 | 12.915 | 14 |
| 9 | 9.3685 | 8.7646 | 10.159 | 10.683 | 11.087 | 11.491 | 12.978 | 12.488 | 13.021 |  |  | , | 12.7 | 13.233 | 13.727 | 14.240 | 16,499 | 1 |
| 10 | 10.462 | 10.950 | 11.464 | 12.006 | 12.578 | 13.181 | 13.646 | 14.487 | 16.193 |  | 14.64 | 4.7. | 15.916 | 15,005 | 18.788 | 17.519 | 20.799 | $u$ |
|  |  |  |  |  |  | 15.181 | 13.616 | 14.487 | 16.193 | 15.337 | 6.722 | 17.543 | 18.420 | 19.337 | 20.304 | 21,321 | 26.959 | ${ }^{2}$ |
| 11 | 11.587 | 12.168 | 12.808 | 13.486 | 14.207 | 14.972 | 75.784 | 16.645 | 17.560 | 18.531 |  |  |  |  |  |  |  |  |
| 12 | 12.683 | 13.412 | 14.192 | 15.026 | 16.917 | 16.870 | 17.888 | 18.977 | 20.141 | 21.384 | 19.661 | 20.666 | 21.814 | 23.046 | 24.349 | 25.733 | 32.150 |  |
| 13 | 13.809 | 14.680 | 15.618 | 16.627 | 17.713 | 18.882 | 20.141 | 21.495 | 22.953 | 24.523 | 26.212 | 24.133 | 5.6150 | 27.271 | 28.002 | 30,850 | 39.581 |  |
| 44 | 14.947 | 15.974 | 17.086 | 18.292 | 19.699 | 21.016 | 22.550 | 24.215 | 26.019 | 27.975 | $\frac{26.212}{30.095}$ | 28.029 | 29.985 | 32.039 | 34.362 | 36.786 | 48.497 |  |
| 16 | 16.097 | 17.293 | 18.699 | 20.024 | 21.579 | 23.276 | 25.129 | 27.162 | 29.361 | 31.772 |  | 32.393 | 34.883 | 37.584 | 40,586 | 43.672 | 59,196 |  |
|  |  |  |  |  |  |  |  | 27.162 | 29.361 | 31.772 | 34.405 | 37.280 | 0,4 | 43.842 | 47.580 | 51.680 | 72.035 |  |
| 16 | 17.258 | 18.639 | 20.157 | 21.825 | 23.687 | 25.673 | 27.866 | 30.324 | 33.003 | 35.950 | 39.180 |  |  |  |  |  |  |  |
| 17 | 18.430 | 20.012 | 21.762 | 23.698 | 25.840 | 28.213 | 30.840 | 33.750 | 36.974 | 40.545 | 48.501 | 42.763 | 6.672 | 50.980 | 55.717 | 60.925 | 87.442 | 18 |
| 18 | 19.615 | 21.412 | 23.414 | 26.645 | 28.132 | 30.906 | 33.959 | 37.450 | 41.301 | 45.599 |  | 48.884 | 53.739 | 58.118 | 65.075 | 71.673 | 105.931 |  |
| 19 | 20.811 | 22.841 | 25.117 | 27.671 | 30,5:9 | 33.760 | 37.379 | 41.446 | 46.018 | 51.159 |  |  |  | 3.3 | 5.8. | 84.141 | 128.117 |  |
| 20 | 22.019 | 24.297 | 26.870 | 29.778 | 33.06i6 | 36.786 | 40.995 | 45.762 |  |  |  |  |  | 8,9 | 88.212 | 98.603 | 154,740 |  |
|  |  |  |  |  |  | 36.786 | 40.096 | 45.762 | $5 \% .166$ | 57.275 | 64.203 | 72.052 | 80.947 | 91.025 | 102.444 | 115.380 | 186.688 |  |
| 23 | 23.239 | 25.783 | 28.676 | 31.868 | 35.719 | 39.983 | 44.885 | 50.423 | 56.765 |  |  |  |  |  |  |  |  |  |
| 22 | 24.472 | 27,298 | 30.537 | 34.248 | 38.6.15 | 43.392 | 49.006 | 55.457 | 62.873 | 71.403 |  | 81.699 | 92.470 | 104.768 | 178.810 | 134.841 | 226,026 |  |
| 23 | 25.716 | 28.845 | 32.453 | 35.618 | 41.430 | 46.996 | 53.436 | 68.893 | 69.532 | 78.643 | 91.148 | 92.603 | 106.4.91 | 120.436 | 137.632 | 157.495 | 271.051 |  |
| 24 | 26.973 | 30.422 | 34.428 | 39.083 | 44.502 | 50.816 | 58.177 | 66.765 | 76.790 | 83,487 | 102.174 | $\underline{118.1656}$ | 120.205 | 136.297 | 168.276 | 183.601 | 326.277 |  |
| 25 | 28.243 | 32.030 | 36.469 | 41.646 | 47.727 | 54.865 | 63.249 | 73,106 |  |  |  | 1133.334 | 136.831 | 168.659 | 184.168 | 213.978 | 392444 |  |
|  |  |  |  |  |  | 54.065 | -3.249 | 73.106 | 64,701 | 98.347 | 114.413 | 133.334 | 165.620 | 181.871 | 212.793 | 249.214 | 471.301 |  |
| 30 | 34.785 | 40.568 | 47.575 | 66,085 | 66.4:19 | 79.058 | 94.461 | 113.233 | 136.308 |  |  |  |  |  |  |  |  |  |
| 35 | 41.660 | 48.994 | 60.462 | 73.652 | 90.320 | 111.435 | 136.237 | 172.317 | 215.711 | 271.02 | 199,021 | 241.333 | 293.189 | 356.737 | 434.745 | 530.312 | , |  |
| 36 | 43.077 | 51.994 | 63.278 | 77.598 | 95.8.36 | 119.121 | 148.913 | 187.102 | 236.125 | 299.127 | 341.630 | 431,663 | 546.681 | 693.573 | 881.170 | - | , |  |
| 40 | 48.886 | 60.402 | 75.401 | 95.026 | 120.a00 | \$54.762 | 199.636 | 269.067 | 337.882 | 299.27 | 380.754 | 484.463 | 618,749 | 791.673 | - | - | , |  |
| 60 | 64.463 | 84.578 | 112.797 | 152.567 | 209.348 | 290.336 | 406.529 | 673,770 | 815.084 | 44. 6 | 681.826 | 767.091 | $\cdots$ | - | * | - | , |  |

