## EASTERN UNIVERSITY, SRI LANKA

FIRST EXAMINATION IN SCIENCE 2005/06 (AUG-SEP. 2007)

FIRST SEMESTER

IBRAR

PH 101 - MECHANICS I

Time: 01 hour. Answer ALL Questions.

1. (a) Define "average velocity" and "instantaneous velocity" and give mathematical expression for both.

A particle located at position x = 0 at time t = 0, starts moving along the positive

x - direction with a velocity v that varies as  $v = kx^{\frac{1}{2}}$ . How do the *displacement*, velocity and acceleration of the particle vary with time t. What is the average velocity of the particle over the first d distance of its path?

(b) A particle is moving in two dimensions and its position is given by the polar coordinates  $(r, \theta)$ . Show that the velocity  $\vec{v}$  and the acceleration  $\vec{a}$  of the particle are given by,

$$\begin{split} \vec{v} &= \dot{r}\vec{e}_r + r\dot{\theta}\vec{e}_\theta \\ \vec{a} &= (\ddot{r} - r\dot{\theta}^2)\vec{e}_r + (r\ddot{\theta} + 2\dot{r}\dot{\theta})\vec{e}_\theta. \end{split}$$

Where,  $\vec{e}_r$  and  $\vec{e}_{\theta}$  are the unit vectors along and perpendicular to the radial direction respectively.

A particle moves in two dimensions  $r = 2\theta$ , where  $\theta$  varies with time t as  $\theta = t^2$ . Show that the acceleration of the particle is  $\vec{a} = 4(1-2t^4)\vec{e}_r + 20t^2\vec{e}_{\theta}$ .

2. Explain briefly what you mean by *kinetic energy*, *power* and *work done by a force*. State "work-energy theorem".

A force F(t) is acting on a particle moving with velocity v(t). Show that the work done W by the force between the time interval  $t_1$  and  $t_2$  is,

$$W = \int_{0}^{t_2} \left(\vec{F} \cdot \vec{v}\right) dt.$$

A force given by  $\vec{F} = (4\vec{i} + 8\vec{j} + 12t\vec{k})$ , acts on a particle of mass 2kg, where the force is in Newton and t is in sec. Assuming that when t = 0 the position vector and the velocity of the particle are zero, find

- i. the velocity and the position vector of the particle when  $t = 1 \sec$ ;
- ii. the work done by the force in the time interval t = 0 sec and t = 1 sec;
- iii. the power of the force at any time t sec.
- iv. Calculate the kinetic energy of the particle when  $t = 1 \sec$  and verify the "Work-Energy" theorem.