EASTERN UNIVERSITY, SRI LANKA SECOND EXAMINATION IN SCIENCE - 2008/2009 SECOND SEMESTER (PROPER/REPEAT) (Sep/Oct 2010) PH 207 ELECTRICITY AND MAGNETISM H 11 FEB 2011

1. Define the terms polarization vector **P** and displacement vector **D** in a dielectric medium.

A spherical capacitor of inner radius *a* and outer radius *b* charged with Q coulomb's. The capacitor is filled with a dielectric, whose dielectric constant varies as: $\varepsilon = \varepsilon_1 + \varepsilon_2 \frac{1}{r^2}$ where ε_1 and ε_2 are constants and $\varepsilon_1 > \varepsilon_2$.

- a) Find the Displacement Vector **D**(r).
- b) Determine the Electric Field **E**(r).
- c) Hence, find the Potential difference V between the spherical cells.
- d) Find the Polarization Vector P(r).
- e) Calculate the Capacitance of the Capacitor.

 (a) Starting with Gauss's theorem in electrostatics, prove the First Maxwell's equation;

$$\vec{\nabla} \cdot \vec{E} = 0$$

(b) State Biot-Savart Law and from this derive the second Maxwell' equation;

$$\vec{\nabla} \cdot \vec{B} = 0$$

(c) State Faradays Law of electromagnetic induction and from the derive the third Maxwell's equation;

$$\vec{\nabla} \times \vec{E} = -\frac{\partial B}{\partial t}$$

(d) State Amperes Circuital Law and from this and using Maxwell' assumptions derive the fourth Maxwell's equation;

$$\vec{\nabla} \times \vec{B} = \mu_0 \frac{\partial \vec{D}}{\partial t}$$

Where the symbols have their usual meanings and assume that the medium is free space.