

Answer all Questions

B.

Time: 03 Hours

01. A. (I) Express the following in its simplest form

(i)
$$\left(x^{3}y^{4}\right)^{2} + \sqrt{x}\left(x^{3} + y^{4}\right)$$
 (ii) $\left(x - \frac{2}{x+1}\right) \div \left[1 - \frac{(4x+7)}{(x^{2}+4x+3)}\right]$

(II) -actorise the following expressions completely

(i)
$$3x^{2n} + 7x^n + 2$$
 (ii) $x^6 + 8y^6$

(III) Solve the following equations

(i)
$$4^x = 8^{3-x}$$
 (ii) $\log(2x+1) + \log(x+3) = \log(12x+1)$.
(60 marks

(I) The manufacturer of a certain product can sell all units at a price of Rs. 20 each. It costs him Rs. 12.50 to produce each item in materials and labour, and he has additional overhead costs of Rs. 7,000 per month in order to operate the plant. Find the number of units he should produce and sell to make a profit of Rs. 5,000 per month.

(15 marks)

(II) A firm manufactures two products P₁ and P₂. Each product has to be processed by two machines M₁ and M₂. Each unit of type P₁ requires 01 hour of processing by machine M₁ and 2.5 hours by machine M₂, and each unit of type P₂ requires 04 hours of machine M₁ and 01 on machine M₂.

Total available time for machine M1 is 400 hours and for machine M2 is 550 hours each month. How many units of each type can be manufactured in one month if the total available time on the two machines is to be utilized?

(25 marks)

Let L be the line passing through the points (-2, -3) and (5, 4).

- (I) Find the slope of this line.
- (II) Find the equation of this line.
- (III) Find the y-intercept point and x-intercept point othis line.
- (IV) Find the intersection point of this line with the line x + 2y = 0.

(50 marks)

- B. Of the equations p + 6q = 420 and p = 6q + 60, one is a supply function of a product and the other is a demand function of that product, where p is the price of the product and q is the quantity of the product.
 - (I) Sketch the two functions on the same axes.
 - (II) Label the demand and supply functions on the graph and ge reasons for your choice.
 - (III) Find the equilibrium price and the quantity.

(50 marks)

03. A. (1) Calculate the matrix C(2A - 3B), where

$$A = \begin{pmatrix} 2 & -5 \\ -3 & 7 \end{pmatrix}, \qquad B = \begin{pmatrix} -1 & -3 \\ -4 & 2 \end{pmatrix} and \qquad C = \begin{pmatrix} 2 & 3 \\ -1 & 5 \\ 7 & -2 \end{pmatrix}$$

(II) If x satisfies
$$\begin{vmatrix} x-1 & 5x-3 \\ 2 & x+1 \end{vmatrix} = 0$$
, find x.

$$A + \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \begin{pmatrix} 3 & 4 \\ -5 & 7 \end{pmatrix} find A.$$

(40 marks)

B. (1) Find the inverse matrix of the matrix,

1	3	5	2)
	2	2	4	
	4	3	4)

02. A.

- (II) A factory makes three different brands of chocolates. Plain-chocolate reduites 3 units of cocoa, 2 units of sugar and 4 units of milk for each box; dark chocolate needs 5 units of cocoa, 2 units of sugar and 3 units of milk for each 60x; and light chocolate uses 2 units of cocoa, 4 units of sugar and 4 units of milk in each box. The factory has stocks of raw materials comprising 4,000 units of cocoa. 3,000 units of sugar and 4,000 units of milk.
 - (a) If x boxes of plain chocolate, y boxes of dark chocolate and z boxes light chocolate are produced in order to use up all of the raw material held in stock, give three linear equations with the three unknowns x, y and z using the information given above.
 - (b) Use the matrix inversion found in (I) to solve the three linear equations.

(60 marks)

IBR

04. A. Differentiate the following functions with respect to x

- (1) $y = (x^3 + 3)^3$ (11) $y = \frac{(1+x)(1-x)}{(x^2 + 1)}$ (11) $y = \log(\sqrt{x} + x)$ (11) $y = x^2(e^x - 1).$
- (40 marks)
- A company producing a single product finds that each item produced cost Rs, 12
 and that it has to pay Rs, 300 in fixed costs each week. If q units are produced each week, write down a function expressing the weekly costs in terms of q.
 - (II) The company operates as a monopoly in a market where the price is given by the function of q.

$$p=24-\frac{1}{20}q.$$

Find the revenue function in terms of q, and hence find the company's profit function.

- (III) Find the value of q that maximizes profits and explain how you can be sure that it is a maximum.
- (IV) Find the maximum profit.

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(V) Find the break-even quantity.

(VI) Suppose that the capacity of the company is limited to 80 units of production per week. It can finance a doubling of capacity by taking out a loan, but the repayments will increase weekly costs to Rs. 400. Decide whether such an expansion will increase profits, justifying your answer.

(60 marks)

05. The annual income data in thousands of rupees for the 30 male policyholders and the 30 female policyholders are shown in the table below.

Class interval	Fre	Frequency	
Class Interval	Male	Female	
15 – 25 📝	8	7	
25 - 35	10	11	
35 - 45	6	5	
45 - 55	3	2	
55 - 65		2	
65 - 75	0	1	
75 - 85	0	2	
85 - 95	2	0	

- (I) Constrict a histogram for the female policy holder salaries and using the same axes construct a frequency polygon for the male policy holder salaries.
- (II) Comment on the differences in the distribution of the male and female salaries.
- (III) Find the following
 - (a) Median salary for male policy holder;
 - (b) Mode salary for female policy holder;
 - (c) Coefficient of variation for male policy holder;
 - (d) Coefficient of variation for female policyholder.
- (IV) From your calculations in (c) and (d) which group had relatively more variation?

(100 marks)